

Monitoring Harness Use in Construction with BLE Beacons

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Abstract

This paper introduces a novel approach to measure and evaluate the proper use of harnesses at construction sites: we deploy Bluetooth Low Energy (BLE) beacons for delimiting areas where the use of a harness is mandatory and to detect whether the harness is attached to the corresponding lifeline when the worker enters these areas. Our method is based on local estimation, through statistical filtering of RSSI measurements (Extended Kalman Filter), of the proximity between the beacons that delimit the different areas and the one in the lifeline, followed by a finite state machine risk status detector. Experiments have been performed in a real construction work-place with a wearable device; their results show that our solution is ideal for dynamic construction environments. Its main advantages are robustness of the detection system, easy relocation of the beacons as the construction zone evolves, and no need for calibration, communication infrastructure, external processing support, or configuration/map updates. Additionally, optional remote IoT for online monitoring is possible.

Keywords: Harness, construction safety, fall from height, beacon, sensor, safety at work.

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Table 1: Main preventive measures against falls from height in the construction sector.

| Strategy | Measure | Authors |
|-------------------------------------|---|----------------------|
| Prevention through Design (PtD) | Safety operations included in the design of the project | [9, 10, 11] |
| Workers' Organization | Work planning Worker training | [13, 14, 15] |
| Collective measures | Safety nets Scaffolding Safety platforms | [16, 17, 18, 19, 20] |
| Personal protection equipment (PPE) | Safety harnesses and lifelines | [21, 22, 23] |

1. Introduction

Occupational accidents in the construction sector continue to give international cause for concern [1]. In particular, falls from height have been identified as a leading cause of fatal accidents in the sector by several authors in many countries, such as the USA [2], Taiwan [3], Spain [4], China[5], Korea[6], Australia [7] or Uganda [8]. Some preventive measures have been proposed to prevent falls from height, and other safety risks, which focus on different strategies. As an example, Prevention through Design (PtD) strategies are based on the inclusion of safety requirements while the project is being designed and not after the design phase [9, 10, 11, 12]. Other authors focus on workers' organization issues such as task planning or safety training [13, 14, 15]. Also, studies about collective measures [16, 17, 18, 19, 20] and personal protective equipment [21, 22, 23] try to mitigate the effects in case of accident, because prevention is not always entirely effective. A compilation of preventive strategies is shown in Table 1.

In construction, not all personal protection equipment is compulsory at every workplace, depending on the risk level in a given zone. Examples of this are harnesses and lifelines :It is not mandatory to connect them at ground level as there is no evidence of any risk of falls from height, but they are mandatory when the worker enters a dangerous zone such as a roof or top floor. According to [24], the problem is that harnesses can be available at the work site but not correctly used.

The introduction of electronic devices in the sector has contributed to improving occupational safety among construction workers. For instance, several technologies such as Radio-frequency identification (RFID) [25], Global

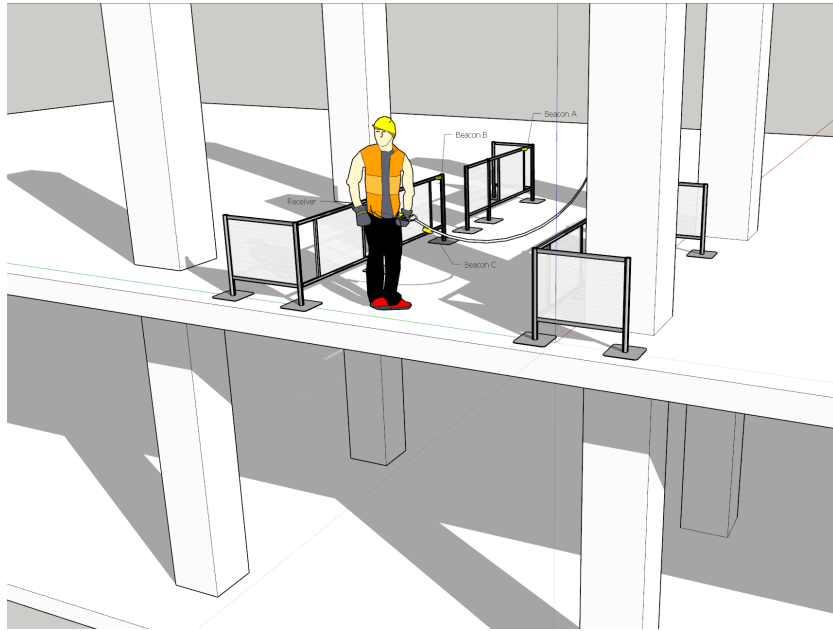


Figure 1: The detection of the use of the safety measures can be done with just three beacons. Beacons A and B are placed in the transition between a safe place and a risk area. A third beacon is located at the lifeline carabiner.

26 Positioning System (GPS) [26] or Ultra-wideband (UWB) [27] have served for
27 the identification, localization and tracking of materials. More recently, simi-
28 lar technologies have been applied in the field of occupational safety to detect
29 personal protection equipment and improve safety conditions [28, 29, 30].

30 Two main wireless technologies are used in work safety applications:
31 RFID and radio-frequency beacons.

32 On the one hand, RFID tags are simple and powered just from the energy
33 captured by their antenna. RFID solutions can be implemented to detect
34 the presence of passive tags [31] in ranges of up to 20 *m*, depending on the
35 frequency, antenna sizes and transmitting power. Near-field communication
36 (NFC) is a subset in the family of RFID technology. They operate at the
37 13.56 *MHz* frequency, within a range of about 30 *cm*, and they have been
38 designed as a secure form of data exchange. An NFC device is capable
39 of being both an NFC reader and an NFC tag. Many smartphones use
40 this technology today for secure payments(a comparative overview of various
41 Body Area Networks can be found in [32]).

Table 2: Comparison of localization technologies. (Adapted from Lin 2013)

| | BLE (Blue- tooth Low Energy) | RFID passive | RFID active | ZigBee | Wi-Fi | GPS |
|------------------------|-------------------------------------|--|---------------------|------------------------|---------------------------------|--------------------------------|
| Power usage | Low | None | Low to medium | Medium | High | Medium |
| Data rate | Low | Low | Low to medium | Medium | High | N/A |
| Coverage | Medium | Low | Medium | High | High | Very high (outdoor) |
| HW costs Advantages | Low price and battery powered | Low price. No battery required in tag | Medium Low price | Medium Low price | High Popular devices (AP) | High Long range coverage |
| Disadvantages | Low preci- sion | Very short range | Low preci- sion | Power con- sumption | High power consumption | Only outdoor workplaces |
| Deployability | Easy | Easy | Easy | Easy | Medium | Easy |
| Accuracy | Poor | Bad | Good | Good | Bad | Bad |
| Maintainability | Good | Good | Good | Good | Bad | Good |
| Stability | Good | Good | Good | Good | Bad | Good |

42 On the other hand, the current standard in radio-frequency beacons is
43 based on the Bluetooth 4.0 specification. It defines the Bluetooth Low Energy
44 (BLE) protocol, that includes the advertising (i.e. beaconing) mode. In this
45 mode, low-power devices broadcast very short messages at a configurable
46 rate that includes the device identification number and the services offered.
47 These messages can be read by any Bluetooth 4.0 or above compatible device
48 without pairing. BLE beacons can continue transmitting for years with a
49 single coin cell battery, thus they are used today as a proximity detection
50 system in commercial, cultural and indoor shops, museums and airports.

51 A comparison of these and other common localization technologies is
52 shown in Table 2. There are two main beacon protocols that provide ad-
53 ditional functionalities to build the Physical Web¹: proprietary protocols
54 from specific vendors like the *iBeacon* from Apple [33], and the *Eddystone*
55 open standard by Google. A survey on the hardware and protocols of the
56 beacons can be found in [34].

57 There are solutions based on RFIDs for the detection of proximity to cer-
58 tain areas (e.g., [30]), but they do not perform continuous monitoring. Other
59 limitations of RFID systems, such as the lack of accuracy and interference
60 with materials, have been also studied in literature [35]. Considering that,
61 our work has been based on radio-frequency.

62 In this paper we introduce a new sensor system for the proper use of
63 harnesses and life-lines in workplaces where it is mandatory due to the high

¹<https://google.github.io/physical-web/>

64 occupational risk levels of fall from height (see the illustration in Figure 1).
65 Our system is composed of an instrumented harness with a BLE receiver, a
66 beacon located at the lifeline carabiner hook, and a set of additional active
67 BLE beacons placed along the risk area entry paths of the workplace. On
68 the software side, a hybrid statistical filtering / finite state machine method
69 deduces both the area in which the worker is located and whether the lifeline
70 has been attached before entering a risk zone, using only the RSSI measure-
71 ments of just three beacons, with minor configuration.

72 The main contribution of this work is thus the use of a simple wearable
73 receiver to detect the current status of the worker, without the need of com-
74 munications or powerful computing infrastructure, and without maps, only
75 using battery-powered beacon pairs that can be easily deployed, relocated
76 and extended as the construction environment evolves. Up to the knowledge
77 of the authors, this is the first method that can be effectively used in con-
78 struction environments for any number of workers and areas since changes
79 can be implemented simply by the physical relocation of the beacons.

80 The structure of the paper is as follows. In section 2, related works are
81 presented. Section 3 describes all the physical components of our system.
82 Section 4 explains the filtering/state-machine method we have implemented
83 for detecting the status of the worker with respect to the beacons. In section
84 5 we discuss the results obtained with our approach. Finally, in section 6 we
85 review the work and propose some future extensions.

86 2. Related works

87 Some form of positioning technology must be implemented to track peo-
88 ple’s positions at the workplace. GPS signals are often unavailable indoors,
89 and the accuracy of public GPS networks is still insufficient for safety applica-
90 tions. Private indoor location systems can use active radio-frequency trans-
91 mitters at known locations; the receiver resolves its position by analysing
92 the attenuation of the signal from each beacon. However, real environments
93 make it difficult to obtain reliable measurements due to attenuations and
94 distances [36].

95 Modern Real-time Locating Systems (RTLS) use various localization tech-
96 niques, including the received signal strength indicator (RSSI), time of arrival
97 (TOA), time difference of arrival (TDOA), and angle of arrival (AOA) [37].
98 We are interested here in the simplest one, RSSI, where attenuations, mea-
99 sured in dB over a milliwatt (dBmW or dBm) are computed in the receiver

100 thanks to the transmission power indications reported by the transmitter.

101 The most common method for estimating the worker's location from the
102 physical measurements is based on triangulation; in that case, RSSI values
103 are considered a function of distance [37]. The problem is that the RSSI
104 signal is very unreliable in a construction workplace due to radio propagation
105 disturbances.

106 Instead of estimating the distance to each beacon based on the theoretical
107 RSSI-distance relationship, fingerprinting methods use a pre-built sampled
108 map of the RSSI values from the different beacons to match the current RSSI
109 signals pattern [36]. Here, the navigation constraints of complex indoor en-
110 vironments can assist these positioning methods to provide higher accuracy,
111 compared with open environments [38].

112 Sensor fusion with information from several sources can provide even more
113 accurate results. For instance, using pedestrian dead reckoning (PDR) and
114 a set of beacons placed on a global map, a 2 m position precision has been
115 obtained [39].

116 An alternative to localization are the so-called proximity methods, that
117 are not aimed at estimating a specific location, but to assess the proximity to
118 a special place, by using special beacons located at trucks, corridors, ladders,
119 etc. [40]. This can also serve to check whether the worker is wearing certain
120 equipment (with a beacon attached to it).

121 Besides the method used, when considering mobile or wearable solutions,
122 size and power consumption have to be taken into account. For instance, in
123 [41] a patent is presented of a method for reducing energy consumption in a
124 tracking device based on the estimation of speed in RF-based localization.

125 The cost of deploying communication infrastructures in non-permanent
126 areas, or the cost of using cellular data networks can be too high. This way,
127 in [42] a method is presented that reduces the reporting of the fingerprints to
128 the location server: the server provides zones with RSS-based representation,
129 and the terminal reports the measurements only when the readings match
130 the configured RSS patterns.

131 Finally, the particular characteristics of construction sites frequently re-
132 duce the suitability of many methods. A global view of the advantages and
133 disadvantages of the previous methods when applied in construction sites
134 are shown in table 3. A system for worker localization and proximity to risk
135 areas in railway construction was proposed by D'Arco [43] based in GNSS
136 and RSSI, but it is not recommended for indoor environments. Other au-
137 thors like Park [40] have proposed to calculate the risk level of the worker

Table 3: Comparison of methods applied in construction sites.

| System | New system | D'Arco (2018) | Park (2017) | Teizer (2007) | Kelm (2013) | Lin (2013) |
|---------------------------------------|---|------------------------------------|-----------------------------------|------------------------------|------------------------------------|---------------------------|
| Applications | Detection of risk area and PPE use at any worksite | Risk areas at Railway construction | Heavy equipment proximity(trucks) | Evaluate worker training | Access and PPE control | Worker behaviour analysis |
| Outputs | Worker risk status considering risk area and PPE attached | Worker location and risk area | Worker risk level | Worker position and velocity | Compliance of mandatory PPE | Worker position |
| Technology used | BLE (RSSI) | GNSS +RSSI | BLE (RSSI)+ Bluetooth / WIFI | UWB | RFID (Active/ Passive) | ZigBee and fingerprint |
| Indoor/ Outdoor | Both | Outdoor | Both | Indoor | Indoor | Both |
| Suitable for dynamics environments | Yes | Yes | Yes | Hard | Hard | Expensive |
| Continuous monitoring | Yes | Yes | Yes | Yes | No | Yes |
| Requires Communication Infrastructure | None | Network | Optional | Network and server | Database access and RFID detection | ZigBee WSN |
| Sensitivity to calibration | Low | Low | High | Very high | None | Very high |
| Local/Global | Local | Global | Local | Global | Local | Global |

138 according to the proximity and movement of heavy equipment (trucks), but
 139 with a high sensitivity of the system to calibration. Worker position and
 140 velocity were obtained in the solution based in UWB proposed by Teizer
 141 [27], although it is hard and expensive to install and calibrate, especially in
 142 dynamic environments.

143 The authors have not found any previous work that monitors the use
 144 of the harness and the closeness to risk zones with so little calibration and
 145 configuration effort as the one introduced in this paper.

146 3. Overview of the solution

147 In this section we describe generally our solution, its electronic compo-
 148 nents and the behavior of the RSSI signal which it is based on. The proximity
 149 detection method is detailed in section 4.

150 3.1. System and components

151 The basic arrangement of our proposal is shown in Figure 2. The wear-
 152 able receiver (R), a Bluetooth Low Energy receiver with a programmable
 153 microcontroller, is attached to the worker's safety harness. Two beacons (A)
 154 and (B) are located on the side of the stairs/corridor that give access to



Figure 2: Two beacons are located in sequence on the side of the entry to the risk area (Left). A third beacon is located on the carabiner that connects the lifeline with the worker harness (Right).

155 the area of the workplace where there is a risk of falling. A third beacon is
 156 attached to the lifeline hook (C).

157 Bluetooth Low Energy is enabled by turning off the radio, using low
 158 standby time, a fast connection and low peak power. The spectrum for Blue-
 159 tooth extends from 2.402 MHz to 2.480 MHz with 40 1 MHz-wide channels,
 160 numbered 0 to 39, separated by 2 MHz. Channels 37, 38, and 39 are the only
 161 ones used for sending advertisement packets periodically. The time interval
 162 between packets has both a configurable fixed interval and a random delay to
 163 reduce the collision probability between advertisements from different devices
 164 [44].

165 Beacons devices from Bytereal Telecommunications International Lim-
 166 ited (HongKong) have been employed in our experiments (See Figure 3).
 167 Based on the Texas Instruments cc2541, these devices are small and provide
 168 BLE with configurable parameters via a mobile application for Android/IOs.
 169 They can operate on single coin cell battery (CR2477) for more than one
 170 year, although their effective life depends on the configured advertising rate.

171 The wearable BLE receiver is based on the powerful and inexpensive
 172 ESP32 chip-set (Espressif Systems, Shanghai, China)², which was designed

²<https://www.espressif.com/en/products/hardware/esp32/overview>



Figure 3: BLE Beacons used in the experiments and a view of the circuit (Left). The receiver (right) is based on an ESP32 chip from Espressif, with Wi-Fi and Bluetooth communications, and powered with a 18650 Li-ion battery. The detection of the lifeline attachment is possible thanks to a commercial BLE beacon placed near the carabiner.

173 for IoT applications. The ESP32 features a Hybrid Wi-Fi and Bluetooth Chip
 174 ESP32 with in-built antenna switches, RF components, and power manage-
 175 ment modules. It is low power and capable of reliable operation in industrial
 176 environments within a wide temperature range (see Figure 3).

177 There is an official open source software development kit in a public repos-
 178 itory for the programming of the device using the Arduino IDE that includes
 179 Bluetooth Low Energy libraries and examples³. The *BLEScan.cpp* software
 180 module has been modified in this work to change its discovery behaviour in
 181 toder to provide continuous scan. Other libraries provide support for Wi-Fi
 182 communications and MQTT protocol functions (Message Queuing Telemetry
 183 Transport) to implement an Internet of Things (IoT) device.

184 3.2. RSSI measurements

185 The BLE API functions provide RSSI values of power for the advertising
 186 messages received during the scan phase. The ESP32 has been programmed
 187 to keep scanning continuously these signals coming from the known beacons
 188 (e.g. Beacons A, B and C) and storing them into a FIFO buffer.

189 RSSI values are noisy and depend on the environment objects and electro-
 190 magnetic interferences, suffering effects such as reflection, refraction, diffrac-

³<https://github.com/espressif/arduino-esp32/tree/master/libraries>

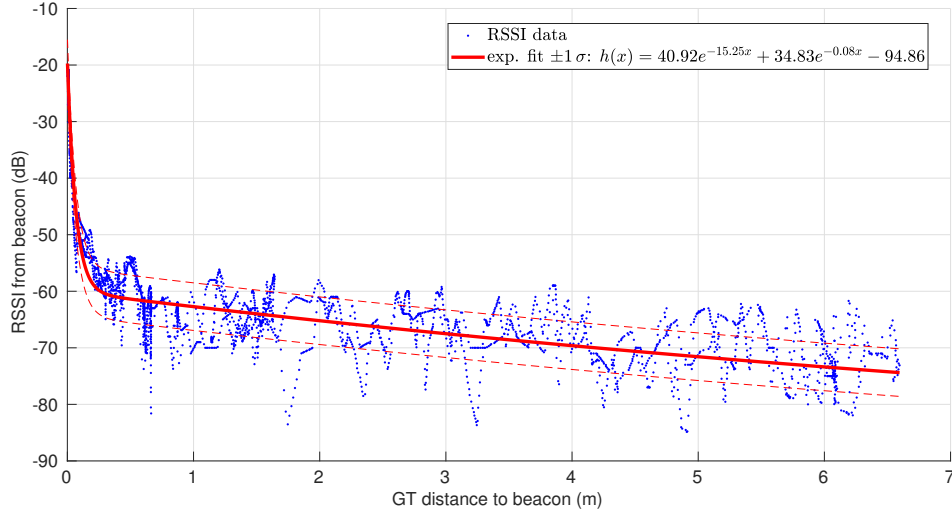


Figure 4: RSSI readings vs. ground-truth distances provided by LIDAR in a scenario where we moved away from the beacon and then came back —hence the two overlapped blue curves of measurements. A theoretical sensor model based on a homoskedastic double exponential fit to the data is also shown:

$$h(x) = ae^{bx} + ce^{dx} - o.$$

191 tion, and scattering. Also, misalignments between the beacon and the re-
 192 ceiver antenna cause polarizations [45].

193 In Fig. 4 a scatter plot of $\simeq 800$ RSSI values gathered from our beacons
 194 at distances from 0 to 5 m is shown, along with a theoretical exponential
 195 model of these sensors.

196 Elsewhere [46], a different model has been used for reporting a relationship
 197 between RSSI values and distances:

$$RSSI(d) = RSSI(d_0) - 10 n \log_{10}(d/d_0) \quad (1)$$

198 which can be considered a two-parameters equation, where $RSSI(d_0)$ is the
 199 RSSI level measured at $d_0 = 1 m$ distance and n is the attenuation parame-
 200 ter. Those parameters are easy to identify from specific beacons in specific
 201 environments; however, this is not suitable for dynamic environments such
 202 as construction, since the RSSI-to-distance conversion is hard to implement
 203 and parameters are changing all the time. Because of this, we use directly
 204 the RSSI values and their previously explained exponential model into the

205 filters of section 4.1 to detect proximity to the beacons.

206 Notice that the different channels will exhibit different attenuations, and
207 thus, different base levels for the RSSI measurements. One of the reasons
208 for the attenuation differences between channels is the multipath interference
209 [47]. This attenuation may change with the distance in up-to -30 dBm in
210 just 10 cm displacements. A beacon transmits every advertising message in
211 the three channels (37, 38 and 39), and a BLE scanner listens in one of these
212 channels sequentially in every scan. BLE libraries do not provide information
213 about the channel used for the received messages, but if the advertising
214 interval matches the scan period (as we do), a sequence of readings is obtained
215 where the same channel is used every three packets, which allow us to address
216 the different attenuation problem.

217 Also notice that the requirements of the application involve a moving
218 target that has to be tracked (the worker), which may lead to additional
219 constraints in the advertising rate of the beacons. As the default scan interval
220 of the wearable receiver is 100 ms, an advertising rate of 100 ms has been
221 selected for all our beacons. Then, a moving window over the last three
222 readings, from which the signal with minimum attenuation is chosen, has
223 been used successfully to get only one RSSI value at a time with consistent
224 attenuation level.

225 4. Description of the method

226 In order to detect the worker status, a proximity detection filter (sub-
227 section 4.1) plus a Finite State Machine (FMS) model of the worker status
228 (subsection 4.2) have been developed and interconnected specifically for this
229 problem.

230 4.1. Development of the proximity detection filter

231 Fig. 5 shows the dynamic Bayesian network (DBN) associated to the
232 estimation problem of the proximity to one beacon when we assume Marko-
233 vianity both in metrical distances and in discrete regions —close/far—w.r.t.
234 a beacon. The random variable r_i represents RSSI measurements, and the
235 two hidden variables d_i and c_i , respectively, the true metrical distance from
236 the worker to the beacon and the belief in the region where the worker is
237 —what we ultimately want to estimate. The variable z_i is required in order
238 to formulate a recursive filter for c_i and it will be explained further on.

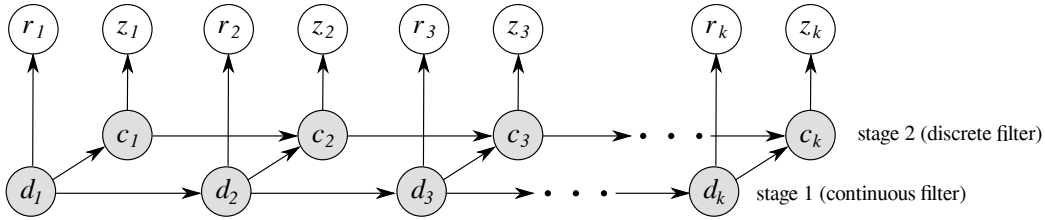


Figure 5: Dynamic Bayesian network for the stochastic processes that govern the changes in the distances of the worker to a beacon (d_i , meters) and in the regions where the worker is believed to be (c_i , far from or close to the beacon). We have also indicated hidden variables (shadowed) and visible variables (not shadowed)

239 Notice that c_i is not a mere consequence of being at a given metrical
 240 distance d_i , but a belief in being close or not to the beacon, something that
 241 also depends on our previous belief c_{i-1} (because it would be unlikely that
 242 the worker leaves and enters the "closeness region" many times in a too short
 243 period of time). Also note that if we wish to use the dependencies between
 244 c_i and c_{i-1} and also keep Markovianity, we need to know (estimate) d_i due
 245 to the structure of this DBN and how d-separation works [48]; otherwise,
 246 $c_i \not\perp c_{1:i-2} | c_{i-1}$. Thus the correct Markovian estimation of c_i in this DBN
 247 must rely on conditioning to d_i .

248 We separate the estimation of the hidden state —the pair (d_k, c_k) into
 249 two parts, each one being solved by a different filter: the first stage is a
 250 Gaussian filter that estimates d_k using observations $r_{1:k}$, while the second is
 251 a discrete filter that uses the results of the first stage for estimating c_k , our
 252 final goal (thus satisfying our condition that we know d_i when estimating c_i).
 253 Although we lose some information about the inter-relations between d_i and
 254 c_i due to this being an approximation to Rao-Blackwellization [49], we have
 255 found that the resulting uncertainty is kept within reasonable limits. This
 256 is also an efficient solution, since the first filter can be implemented with an
 257 EKF [50] (an Extended Kalman Filter is required because the observation
 258 model, as it was shown in Fig. 4, is non-linear).

259 In order to set up this double filter, the second stage —the discrete filter
 260 needs some non-hidden observation to do its estimations. We do not have
 261 such a "sensor", but when we are estimating c_i we have already estimated
 262 d_i , therefore we can approximate the missing sensor by generating "virtual
 263 observations" z_i from the estimates of the first filter. We have chosen the
 264 z_i variables to be the probability of the estimate EKF_i to be closer than a

265 given threshold τ_c from the beacon ($z_i = cdf_{EKF_i}(\tau_c)$). We have used 70 cm
 266 for that threshold ($\tau_c = 0.7$) in our experiments after checking out that the
 267 worker never gets closer than 60 cm to the beacons.

268 With all these considerations, we can now formulate both filters. The
 269 first stage (EKF) is governed by the following system state model:

$$\begin{aligned} d_k &= d_{k-1} + \epsilon_k, & \epsilon_k &\sim N(\epsilon_k; 0, Q_k) \\ r_k &= h(d_k) + \delta_k, & \delta_k &\sim N(\delta_k; 0, R_k), & \epsilon_k &\perp \delta_k \\ h_k(x) &= ae^{bx} + ce^{dx} - o \end{aligned} \quad (2)$$

270 where $h(\cdot)$ is the observation model, i.e., the exponential that we depicted
 271 in Fig. 4. Note that the dynamics of this system does not use any motion
 272 information (our goal b)), thus the transition from one state to the next
 273 is modelled as Gaussian stochastic perturbations, also called a *non-motion*
 274 *model* [49].

275 For the implementation of the EKF we need to provide concrete values for
 276 Q_k , the Jacobian of h_k and R_k . The two latter ones are just the derivative of
 277 $h_k(x)$ and the variance of $h_k(x)$ when x is instantiated with a particular value,
 278 respectively, both already defined in our observation model. Regarding Q_k ,
 279 under the *non-motion model* of transition it is known that⁴ $Q_k = \hat{v}_{max}^2 / \chi_{1,\alpha}^2$
 280 if the expected maximum speed of the system (the worker in this case) is
 281 \hat{v}_{max} with a probability of $1 - \alpha$. In our case we have chosen 0.5m/s as the
 282 maximum worker speed at all times with 95% of probability ($\alpha = 0.05$), thus
 283 we obtain $Q = 0.067$.

284 As for the discrete filter, it updates a posterior on a binary variable ($c_k \in$
 285 {close, far}) according to a recursive Bayesian formulation:

$$\underbrace{P(c_k | z_{1:k}, d_{1:k})}_{\text{posterior at } k} \propto \underbrace{p(z_k | c_k)}_{\text{likelihood}} \underbrace{\sum_{c_{k-1}} \underbrace{P(c_k | c_{k-1}, d_k)}_{\text{transition}} \underbrace{P(c_{k-1} | z_{1:k-1}, d_{1:k-1})}_{\text{posterior at } k-1}}_{\text{prior}} \quad (3)$$

286 In practice, between successive iterations of the filter we only have to store
 287 the posterior for $c_k = \text{close}$, since the belief in being far from the beacon is 1
 288 minus that.

⁴The factor $\chi_{1,\alpha}^2$ is the value in the support of the chi-squared distribution with 1 degree of freedom that marks the beginning of an upper tail that has exactly an area of α .

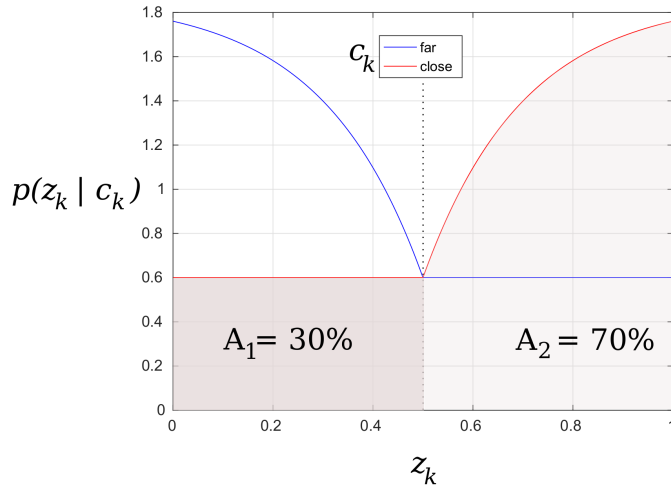


Figure 6: Likelihood function for the discrete filter, i.e., $p(z_k|c_k)$, for the two cases of c_k (worker far/close to the beacon = blue/red respectively).

289 The support of the likelihood probability distribution of this discrete filter
 290 is $z_k \in [0, 1]$, and we assume that c_k is known when evaluating it, i.e., the
 291 worker is believed to be either far or close to the beacon. Fig. 6 illustrates
 292 our definition of that likelihood. When we assume that the worker is close
 293 to the beacon, it is unlikely that the probability of being closer than τ_c
 294 is low ($z_k \in [0, 0.5]$), thus we have set a small uniform likelihood; in the
 295 same situation, observing higher and higher probabilities of being closer than
 296 τ_c to the beacon will be more and more likely, which, for the sake of a
 297 gradual evolution on those likelihoods, has been modelled as a first-order
 298 linear system response. The parameters of that first-order system response
 299 have been chosen to obtain an overall probability of getting large z_k of about
 300 70% vs. a probability of observing small z_k of about 30%. The case of the
 301 worker being far from the beacon is naturally symmetric to this one (blue
 302 curve in the figure).

303 The transition of our discrete filter, $P(c_k|c_{k-1}, d_k)$, is a discrete *pmf* that
 304 depends on both the previous region and the current distance to the beacon.
 305 c_{k-1} will be instantiated with every possibility in the sum of eq. 3, but
 306 we do not know d_k (it is hidden); we use its estimate, produced by the
 307 EKF, instead, thus obtaining an approximation. For defining completely
 308 this approximate transition we use $P(c_k|c_{k-1})$ modulated by the evidence of

309 d_k , as follows: $P(c_k|c_{k-1})$ is increased linearly if the evidence provided by
 310 the estimate of d_k supports the particular combination of c_{k-1} and c_k , and
 311 is decreased linearly when that evidence contradicts it (it is not modified
 312 if $d_k = \tau_c$, the threshold we use to distinguish far from close). As for the
 313 values of $P(c_k|c_{k-1})$ needed to do these operations, we have filled in its 2 x
 314 2 table after observing several experiments in which the worker passed by
 315 a beacon in a representative path; in these experiments the probability of
 316 changing from being close to the beacon to being far from the beacon in one
 317 measurement step is believed to be 3,23%, and the one of changing from far
 318 to close 0,72%. The other values of the $P(c_k|c_{k-1})$ table have been deduced
 319 from the fact that $\sum_{c_k} P(c_k|c_{k-1}) = 1, \quad \forall c_{k-1}$. Obviously, the mentioned
 320 values can be easily tuned for different environments and worker behaviours.

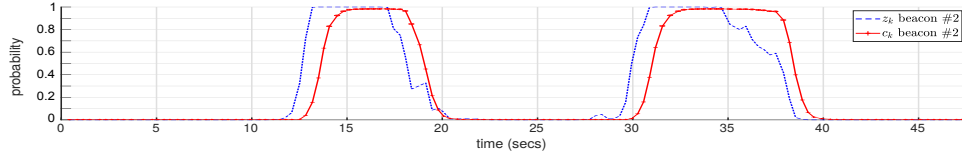
321 The final information needed to execute both filters is the prior distri-
 322 butions for d_0 and c_0 . These are not critical either, since the filters usually
 323 converge in few steps. In the experiments shown in the next sections we have
 324 chosen values compatible with the scenarios, in particular for the worker be-
 325 ing initially around $\pm 10cm$ from the true distance from the beacons with
 326 95% probability and, consequently, in state $c_0 = \text{far}$ with 100% probability.

327 Fig. 7 shows the results obtained with our double continuous + discrete
 328 filter in a real scenario where a worker passes by a beacon twice. In spite of
 329 the noisy RSSI measurements, the EKF is able to track the true distance to
 330 the beacon quite well; more importantly, the noisy estimates of z_i (red line
 331 in Fig. 7(b)), which only depend on the metrical distances d_i , are smoothed
 332 through the discrete filter, obtaining a quite robust and clean "closeness"
 333 signal (red line in Fig. 7(a)).

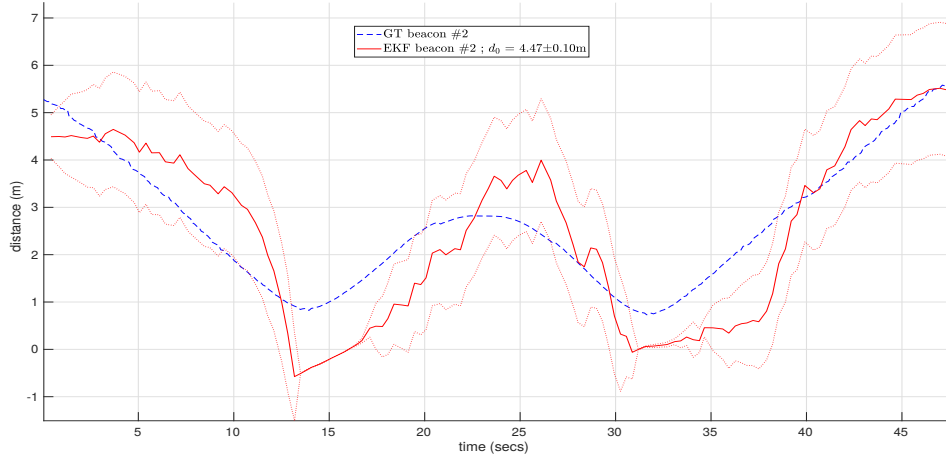
334 4.2. Status detection method

335 Based on the filtering process of subsection 4.1, we can detect whether
 336 the worker is going through risky situations. The minimum infrastructure
 337 for such detection is based on three different beacons as shown in figure 8.
 338 Beacons A and B are placed in the transition between a safe place and a
 339 risk area. A third beacon (C), located in the carabiner of the lifeline, is used
 340 to detect the connection between the harness, where the receiver is located,
 341 and the lifeline. The location of the worker with respect to the beacons is
 342 computed based on the output of the discrete filter described in subsection
 343 4.1. That filter provides closeness detection in the form of a probability.
 344 We have used a reasonable threshold T (e.g. 0.75) on the belief of being
 345 close than τ_c to decide proximity to a particular beacon. If the status of the

a) Discrete filter



b) Continuous filter



c) RSSI measurements

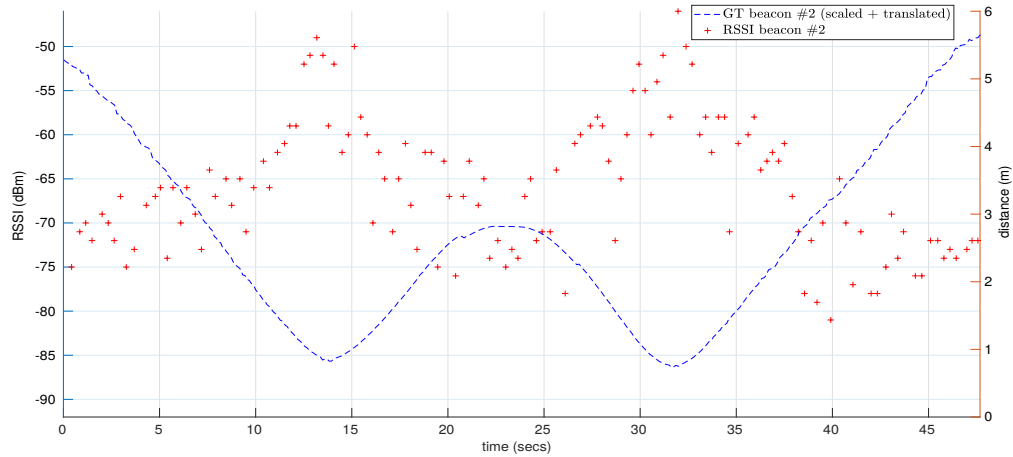


Figure 7: Results obtained by our double filter solution for estimating the "closeness" of the worker to a beacon. a) Estimates of z_i (blue) and c_i (red). b) EKF estimates of the metrical distance of the worker to the beacon (red) superimposed to the ground-truth provided by the LIDAR. c) RSSI measurements gathered along the worker path, who passes by the beacon twice (ground-truth estimates measured by the LIDAR are also superimposed for reference).

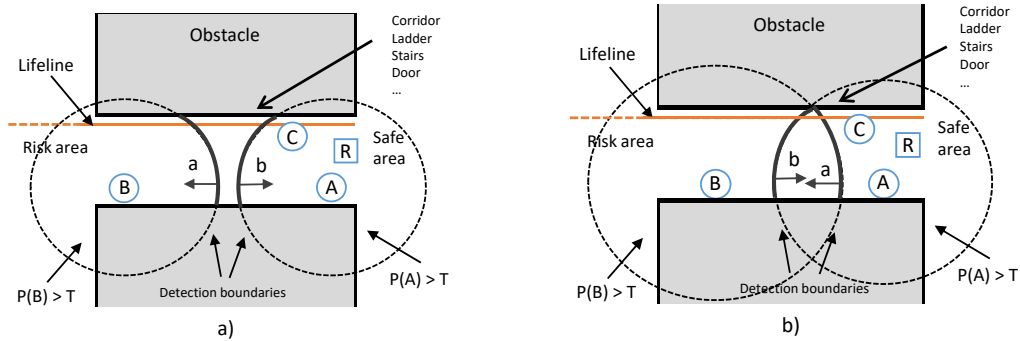


Figure 8: Beacons A and B placed in the transition between a safe place and a risk area. Beacon C is attached to the lifeline hook and the receiver (R) moves along the area. In a) A and B beacons have separated proximity areas delimited by the proximity threshold T . In b) beacons A and B have overlapped proximity areas.

346 last closeness decision is kept, large areas can be detected, as long as all the
 347 accesses are properly beaconized.

348 The distance between beacons A and B define whether proximity areas
 349 are separate or partially overlapped. In Figure 8a) beacons A and B have
 350 overlapped proximity areas, while in Figure 8b) areas are only partially overlapped.
 351 A distance between 1 and 2 m between beacons has been used in our
 352 experiments.

353 The worker status detection method can be modelled as a Finite State
 354 Machine (FSM) as shown in Figure 9. The detector has three states (0, 1 and
 355 2). The transition conditions are based on the output of the discrete filter
 356 presented in subsection 4.1 for each beacon.

357 Local notifications of the worker status are produced by using a red LED
 358 when the worker is in status 0 or 1, and with an acoustic signal when the
 359 worker status is 2.

360 4.3. Remote monitoring

361 Although local user notification and data logging of the status of the
 362 harness utilization works autonomously on the wearable receiver, additional
 363 external monitoring can also be included via IoT clients that offer real-time
 364 information of the state of every wearable in the construction site. In the absence
 365 of a Wi-Fi infrastructure, a cellular module (e.g. GPRS or 3G) can be

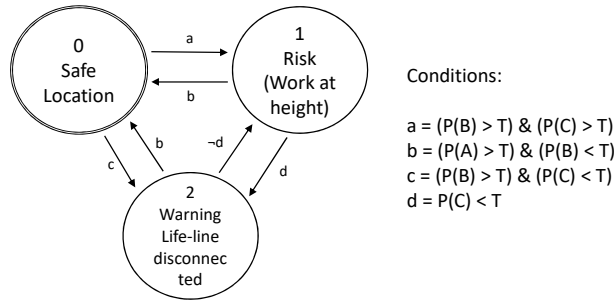


Figure 9: State diagram for the harness status identification FSM. Each transition is triggered by conditions a to d based on the filtered RSSI measurements from beacons A, B and C and the proximity signal threshold T .

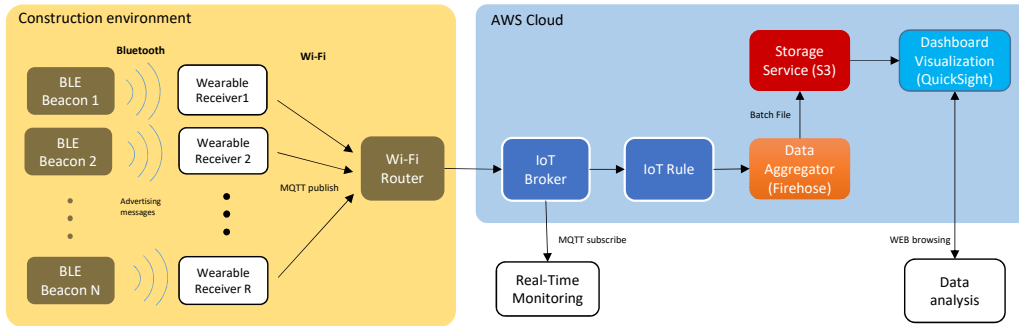


Figure 10: IoT architecture for the optional monitoring and data visualization of the receivers information.

366 added to the wearable and programmed using available PPP-over-Serial pro-
 367 tocol (PPPoS) libraries. This way the wearable receiver publish the worker
 368 status to a IoT broker using an M2M lightweight protocol such as MQTT.
 369 Only status changes have to be published, thus reducing communications
 370 cost and power consumption.

371 For instance, monitoring dashboards of the IoT data (wearable locations,
 372 status and even RSSI data from every device) for further analysis can be
 373 built on the Amazon Web Services (AWS) platform using the *Quicksight*
 374 service. There, an IoT rule provides relevant MQTT messages to an aggregator
 375 (*Kinesis FireHose*) that store data sets in the *S3* storage service as shown
 376 in Figure 10.

377 5. Discussion of results

378 Three different scenarios have been tested to validate our method, where
379 a worker with the wearable receiver walks along a 10 *m* by 2 *m* corridor that
380 connects the safe area with the risky area, with different usage of the safety
381 measures. Beacons A and B are placed in the middle section of the corridor
382 with a separation of 2 *m*, located at a distance of 6 *cm* from the wall, and at
383 a height of 115 *cm* from the floor. Transmitters were configured to advertise
384 at intervals of 0.1 *s*. Beacon A is located at the safe side of the corridor,
385 where the lifeline hook must be attached by the worker, while beacon B is
386 located at the risky side, where the work at height begins.

387 The wearable receiver is fixed to the worker's safety harness, next to
388 the carabiner. The third beacon (C) is installed on the lifeline hook lead
389 (initially next to beacon A); that hook has to be attached to the harness
390 with the wearable receiver, at all times, by the worker, while working at the
391 risky side.

392 In order to get ground-truth data to validate and illustrate the results
393 of our methods, an experimental setup has been built using an external
394 computer and a LIDAR sensor on a wheeled platform, and a procedure to
395 compute the distance between the receiver and the beacons has been pro-
396 grammed. The wheeled platform carries an inexpensive RPLidar A2 sensor
397 by SlamTec⁵, the BLE receiver and the computer. Measurements from the
398 receiver and the LIDAR sensors have been synchronized and a Matlab script
399 has been used to convert LIDAR scans into positions.

400 For each experiment, two graphs have been obtained; a time plot and a
401 2D plot of the path followed by the receiver. The time plot shows three types
402 of data: raw RSSI measurements for each beacon; probability of proximity
403 to each beacon; and results of the FSM, that gives the harness status based
404 on the probabilities and a threshold.

405 The 2D path followed by the wearable receiver has been plotted over a
406 map, with different sections and colours according to the harness status com-
407 puted by the FSM described in section 4.2. Time labels have been added to
408 match the changes in the closeness status with the time plot of the readings.
409 A blue path indicates that the worker is in a safe area (state 0). Red indi-
410 cates a risk area (state 1). Black has been used to indicate that the lifeline
411 has been disconnected in a risk area (state 2).

⁵<https://www.slamtec.com/en/Lidar/A2>

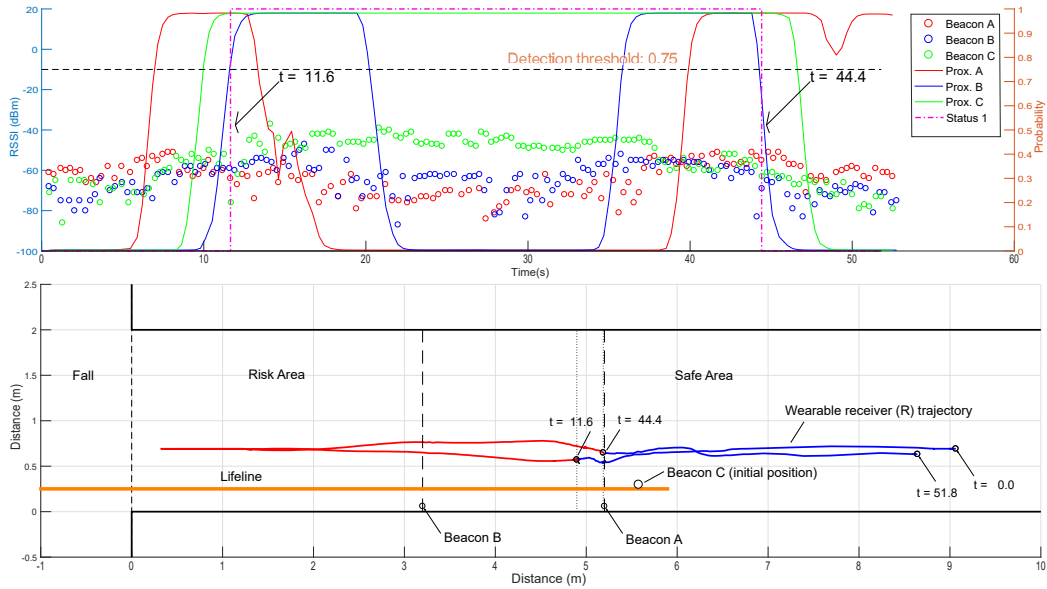


Figure 11: Scenario 1. The worker travels along the corridor attaching the harness at the beginning of the work at height and disconnecting it at the end. (Up) Raw RSSI data and output of the discrete filter. (Down) 2D trajectory of the worker on the corridor map.

412

413 5.1. Scenario 1. Proper use of the safety harness

414 In experiment 1 (see Figure 11), a proper use of PPE is shown, where
 415 the worker approaches beacon A and attaches the safety harness. Then he
 416 continues at a distance of approximately 70 cm from beacon B. The detection
 417 status is changed at $T = 11.6$ s indicating that the worker is in the risk area,
 418 but with the safety measures on. After reaching the end of the corridor, he
 419 returns to beacon A in $T = 44.4$ s, where the safety harness is disengaged
 420 from the lifeline carabiner.

421 5.2. Scenario 2. Harness disconnected in the middle of work at height

422 In experiment 2 (see Figure 12), a common, but illegal, use case is tested.
 423 Here, the worker attaches the lifeline by the beacon A, but the lifeline is
 424 temporary disconnected while working at the risk area. Once reconnected,
 425 the worker returns to the starting point and disengages the lifeline again.
 426 This situation was recognized as a normal case in $T = 16.0$ s, but the violation

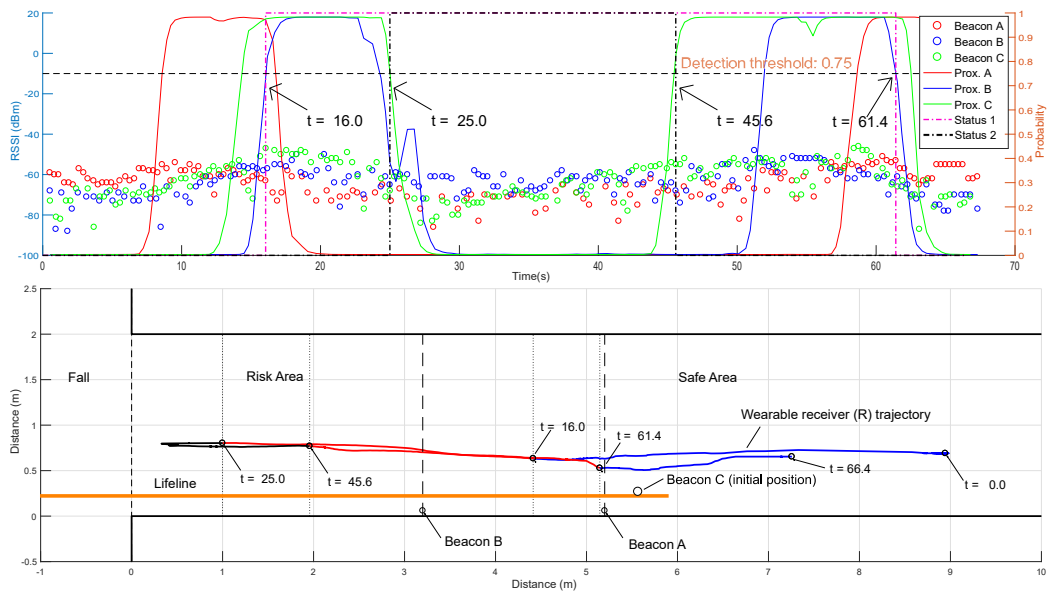


Figure 12: Scenario 2. Task where the harness is disconnected in the middle of work at height. (Up) Raw RSSI data and output of the discrete filter. (Down) Trajectory of the worker along the corridor map. The black section shows the illegal section in black.

427 is detected at $T = 25.0$ s until $T = 45.6$ s. This has been shown in Figure
 428 12(Down), where the risky path section is drawn in black.

429 In this case, acoustic local notification can be used to notify the worker
 430 and a log of events stored in the device can be analysed for later assessment
 431 of the use of PPE.

432 5.3. Scenario 3. Lifeline not used

433 Here (see Figure 13), the worker walks along the corridor, passing in
 434 front of the beacons A, B, and C at a distance of approximately 1 m without
 435 connecting the harness to the lifeline. The lifeline beacon (C) is detected
 436 twice, but as the worker moves away from it, the FSM changes the status to
 437 illegal (status 2) between $T = 15.4$ s and $T = 36.8$ s.

438 6. Conclusions and future work

439 The system proposed in this paper, based on the use of BLE beacons for
 440 the location of workers in the workplace and of efficient statistical filtering

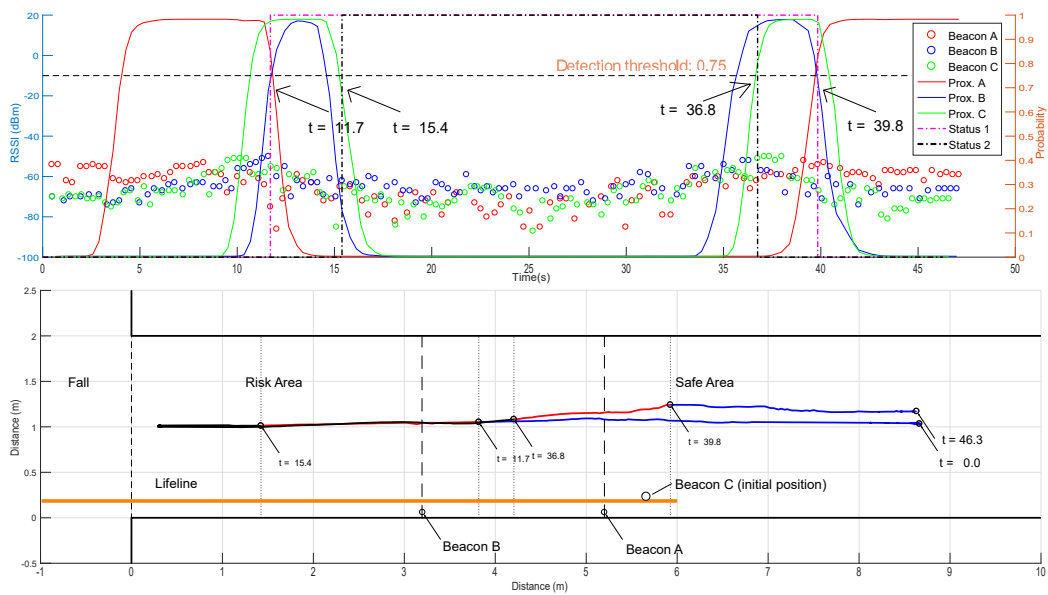


Figure 13: Scenario 3. Task example where the lifeline has not been connected to the harness. The lifeline beacon has been detected as the worker passes by, but the illegal status is detected when the worker enters the risk area. (Up) Raw RSSI data and output of the discrete filter. (Down) Trajectory of the worker along the corridor map

441 for processing their data, has been proved to be an effective tool for detecting
442 robustly whether the worker is located in a place where harness and lifelines
443 are mandatory and whether these are being used properly.

444 The system can be installed in corridors, stairs, ladders, etc., and requires
445 minimum configuration and infrastructure (just tree beacons per boundary).
446 There is no need for communications networks or maps, and can be easily
447 relocated, making it ideal for very dynamic environments such as construction
448 sites.

449 The experiments presented have been based on the minimum set of bea-
450 cons, but this system can be applied to any number of areas and workers.
451 The use of a special advertising ID for the A, B and C-type beacons allows
452 us to create unlimited virtual boundaries without maps or configuration of
453 the electronic devices. Special labelling or colour coding on the beacons can
454 make this deployment easier. Also, accuracy can be improved by increasing
455 the number of beacons in the system.

456 The maximum distance to the beacons that has been tested is around 1
457 m. Higher distances can be achieved by using multiple A-B beacons (e.g. in
458 both walls of the corridor) or using antennas with higher gain. The distance
459 between beacons has been chosen experimentally. In future work we have to
460 study the use of shorter distances to reduce the transition distance for
461 shorter corridors.

462 As the wearable receiver antenna varies the polarization angle against the
463 transmitters antennas as the user moves, changes in the attenuation of the
464 signals can occur for a given distance. Solutions using multiple receivers [51]
465 with different orientations for RSSI stabilization are too bulky and would
466 add too much complexity. The use of new compact MIMO antennas for
467 Bluetooth [52] would reduce the multi-path propagation effects but do not
468 avoid the attenuation caused by the human body proximity. In that sense,
469 the use of multiple A-B beacons would help to get a more reliable estimation.

470 Our method not only provides local real-time detection of the use of
471 harness by workers in zones designated as dangerous, but also allows for
472 remote monitoring, which would provide improved coordination of safety
473 conditions and proper execution of dangerous tasks. The (small) detection
474 delay due to the causal filters for the local real-time detector can be removed
475 when using RSSI data for remote off-line analysis. Remote control of the
476 safety measures in real time can lead to improvements in safety conditions
477 for dangerous tasks. Coordination and planning of tasks can be updated
478 with real input from people working in dangerous zones.

479 According to the manufacturer, the beacon batteries can last for more
480 than a year, and are easily replaceable. Moreover, as the receiver scan bea-
481 cons messages in passive mode, a Li-Ion 18650 battery can last for more than
482 one day without charging.

483 This method is a step toward the development of infrastructure-less or
484 device-free methods in the future, as suggested by [38].

485 *6.1. Impact on construction sector*

486 The economic impact of our system is very small when compared with
487 the total budget of the majority of construction projects. Cost of beacons
488 and receptor range from 10 to 20 Euro per unit. Environmental impact is
489 also low because beacons and receptors can be re-used once the works has
490 been finished.

491 Traditionally, the construction sector has proved to be a sector resistant
492 to the introduction of technological changes when compared with other in-
493 dustrial sectors. Support from company directors and management will be
494 necessary to ensure successful implementation and use of the system pro-
495 posed. Workers' privacy and the opposition of some workers to being located
496 continuously could act as an obstacle. Considering the system as an effective
497 safety tool could reduce initial resistance on the part of workers.

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