

30 **Abstract**

31 We evaluated three definitions of heat wave (HW), and demonstrate that selection of the
32 reference period and air temperature threshold used in the definition can affect the
33 reported frequency of HWs. First, we propose an alternative definition of HW that is
34 based on a moving reference period and specific air temperatures threshold for each
35 calendar date. Then, we present a case study using data from 5 observatories in Malaga
36 Province (Spain) from 1971 to 2016. We assessed the effect of a moving reference
37 period (rather than a fixed reference period) and the definition of daily air temperatures
38 threshold on the identification of anomalies in the definition of a HW. The results
39 indicate that HWs can occur throughout the year. Finally, we propose incorporation of
40 minimum daily air temperatures in two alternative definitions of HW. Our results
41 indicate a high frequency of HWs in the summer months, in which HWs are mainly due
42 to anomalous high T_{min} and more frequent HWs in which maximum and minimum
43 daily air temperature are exceeded from 2014 onwards. These new methods of defining
44 a HW provides more accurate assessments of thermal discomfort.

45

46 **Key words:** daily threshold, heat waves, maximum air temperature, minimum air
47 temperature, moving reference period.

48

51 **1. Introduction**

52 There is increasing attention devoted to changes in climate variability and in the
53 extremes of weather and climatic events (Houghton *et al.*, 2001). Relative to changes in
54 mean climatic variables, changes in extreme climatic events have a greater impact on
55 human activities, the natural environment, agriculture, and insurance coverage (Kunkel
56 *et al.*, 1999). More specifically, changes in the frequency or/and intensity of extreme
57 events have affected human health directly (*via* heat and cold waves) and indirectly (*via*
58 floods or pollution) (Zwiers and Kharin, 1998).

59 The term 'heat wave' (HW) originates from the first descriptions of hot periods
60 recorded in the 1930s in the United States, and one of the first HWs mentioned in
61 scientific papers occurred in Saint Louis in 1936 (Ellis and Nelson, 1978). Until the
62 1970s, most research concerning HWs were carried out in the United States. Over the
63 next few years, the first descriptions of HWs and extreme air temperature values in
64 Europe appeared (Kuchcik, 2006). Increasing interest in the occurrence of observed
65 HWs is substantial and not solely because of global warming. Persistent periods of very
66 high temperature have a strong impact on human health (Tomczyk and Bednorz, 2016).

67 Nonetheless, there is no one objective and uniform definition of HW (Tomczyk
68 *et al.*, 2017a). In China, heat warnings are issued when maximum temperature is
69 forecast to exceed 35°C on any one day, while in the United Kingdom, regionally
70 varying thresholds of maximum and minimum temperature must be exceeded for two
71 consecutive days and an intervening night. The Netherlands meteorological bureau
72 issues warnings to health services when maximum temperatures are predicted to exceed
73 25° C for at least 5 days of which at least 3 days threaten temperatures above 30°C. In
74 the United States, the National Weather Service suggests early warning when the
75 daytime heat index (including adjustment for humidity) reaches 40.6°C and a nighttime

76 minimum temperature of 26.7°C persists for at least 48 h. (Gershunov et al., 2009). The
77 scientific community considers a summer HW event as a prolonged sequence of days of
78 excessive heat over a large area (Chen *et al.*, 2017) or as an isolated episode in the
79 summer with an extremely high near-surface air temperature that lasts several days or
80 more (Robinson, 2001; Lau and Nath, 2012; Shevchenko *et al.*, 2014).

81 The number of HWs has increased worldwide in recent decades (Shevchenko *et*
82 *al.*, 2014), and there were extreme HWs in Western and Southwestern Europe during
83 June and August of 2003 (Fink *et al.*, 2004; Rebetez *et al.*, 2006) and during June and
84 July of 2006 (Fouillet *et al.*, 2008; Gosling *et al.*, 2009; Rebetez *et al.*, 2009; Kyselý,
85 2010; Monteiro *et al.*, 2013). A particularly extreme HW occurred during July and
86 August of 2010 in Eastern Europe and Western Russia (Barriopedro *et al.*, 2011;
87 Grumm, 2011; Rahmstorf and Coumou, 2011; Otto *et al.*, 2012; Shevchenko *et al.*,
88 2014). From 2011-2015, no HW had an impact as extreme as the 2003 HW in Central
89 Europe or the 2010 HW in the Russian Federation, although there were intense HWs
90 during that period (WMO, 2016). In Eastern and Central Europe, the most serious HW
91 since 2003 was during the first half of July in 2015. According with Hoy et al., (2017)
92 the extreme summer of 2015 was characterized by very intensive heat episodes with
93 extreme or even record high temperatures in large parts of Europe. A study on extreme
94 European summer heat waves by Russo et al. (2015) ranked the 2015 heat event as sixth
95 severe since 1950, combining heat intensity and spatial extent. At that time, Germany
96 had national record air temperature of 40.3°C; several weeks later, there were
97 unprecedented record high air temperatures in Spain, France, and Switzerland. This was
98 the longest recorded HW in Spain, which experienced the warmest July since the
99 beginning of record keeping, and there were similar events in Switzerland and Austria.

100 There were also significant HWs in different parts of Europe during the summers of
101 2012, 2013, and 2014 (WMO, 2016).

102 It is likely that the frequency of HWs has increased in Europe, Asia, and
103 Australia since 1950, according to Intergovernmental Panel on Climate Change (IPCC)
104 (2013). Other research indicates that HWs will become more frequent and intense in the
105 future due to global warming (Meehl and Tebaldi, 2004; Christidis *et al.*, 2005; Hansen
106 and Sato, 2012; Coumou and Robinson, 2013; Watanabe *et al.*, 2013; Lee and Lee,
107 2016, Chen *et al.*, 2017). These forecasted changes have motivated weather forecasters
108 to develop more accurate methods to identify and predict HWs, so that society can
109 mitigate their impact (WMO, 2011; Coumou and Rahmstorf, 2012; Lee and Lee, 2016).

110 Statistical analyses of the characteristics of HWs examined data from many
111 countries including China (Tan *et al.*, 2007), Czech Republic (Kyselý, 2002), France
112 (Fouillet *et al.*, 2008), Portugal (Monteiro *et al.*, 2013), Spain (Díaz *et al.* 2006), and the
113 USA (Gershunov *et al.*, 2009), particularly after extreme events (Shevchenko *et al.*,
114 2014). However, these studies of anomalies only considered data from the summer
115 months.

116 HWs are a natural hazard, and much is known about their effects on the human
117 body (Kovats and Hajat, 2008). In particular, they have significant impacts on the well-
118 being, efficiency, and health of humans, and can lead to marked short-term increases of
119 morbidity and mortality (Kovats and Ebi, 2006; Basu, 2009; Gosling *et al.*, 2009), and
120 their effects are particularly significant in cities (Shevchenko *et al.*, 2014). The
121 adaptation and vulnerability of the population to heat waves depend on the local average
122 temperatures and on the frequency of heat waves (Donaldson *et al.* 2003; Pascal *et al.*,
123 2006). Deadly heat waves have always been associated with elevated night-time
124 temperatures (Besancenot 1990a; Diaz *et al.* 2002a, 2002b).

125 The total impact of a HW, which can jeopardize human health and lead to losses
126 in economic sectors such as agriculture and forestry, depends on its magnitude and
127 timing and also on the adaptability of humans and public health responses (Shevchenko
128 *et al.*, 2014). The impact of such events is greater when there are extreme weather
129 conditions over extended periods, and this is the reason for the increased focus on HWs.

130 An improved understanding of the dynamical and physical processes of HWs is
131 needed to improve our ability to predict these phenomena, and to develop strategies that
132 can reduce their impact on human health and agriculture (Lee and Lee, 2016). Robinson
133 (2001) concluded there is no consensus regarding a strict definition of HW. Current
134 definitions of HWs from Spain's State Meteorological Agency (AEMET) only consider
135 air temperatures during July and August, relative to a fixed reference period, to establish
136 a common air temperature threshold for air temperature anomalies on any calendar date.
137 These criteria do not consider air temperature anomalies at other times of the year, what
138 are referred as warm spells (Tomczyk *et al.* 2017b). Moreover, because of the increase
139 in mean air temperatures over time, the threshold for a HW may need to be modified.
140 Other definitions of a HW, such as that from the IPCC, attempt to overcome some of
141 the drawbacks of the AEMET definition, but most continue to rely upon a fixed
142 reference period.

143 We propose an alternative definition of HW that is based on a moving reference
144 period and specific air temperatures threshold for each calendar date, and then evaluated
145 the frequency of HWs according to this new definition. We also suggest two more
146 definitions of HW that consider maximum and minimum daily air temperatures, and are
147 based on a moving reference period and specific threshold air temperatures for each
148 calendar date. Then we determined the annual HW series at five observatories in
149 Malaga Province (Spain), and compared these series to the HW series determined by the

150 AEMET and IPCC definitions.¹ We also analyzed the monthly frequency distribution of
151 HWs throughout the year according to each proposed definition.

152

153 **2. Factors used to define heat wave: first proposal**

154 We analyzed the effect of the reference period and the definition of threshold air
155 temperature on the identification of air temperature anomalies used to define HWs. The
156 criteria used to define a HW often depend on the aims of a study and the available
157 meteorological data (Gershunov *et al.*, 2009; Antics *et al.*, 2013; Pascal *et al.*, 2013).
158 AEMET currently defines a HW as “a spell of at least three consecutive days, in which
159 at least 10% of the observatories considered are above the 95th percentile of its series of
160 daily maximum air temperatures (Tmax) of the months of July and August of the period
161 1971-2000.” There are other definitions of a HW, such as that from the IPCC that
162 defines a HW as a period of more than 5 consecutive days with daily Tmax of 5°C or
163 more above the mean daily Tmax for the normal climatic period 1961–1990 (Frich *et*
164 *al.*, 2002; Radinovic and Curic, 2012).²

165 We propose modification of 2 aspects of the definition of AEMET, so the term
166 HW can provide a more meaningful measure of current weather conditions. First, the
167 AEMET definition relies on daily Tmax values over a fixed 30 year time period. The
168 World Meteorological Organization (WMO) mandates each member nation compute
169 30-year averages of meteorological quantities at least every 30 years (1931–1960,
170 1961–1990, 1991–2020, etc.), but it also recommends an update every 10 years (Arguez
171 and Russel, 2011).

172 The use of daily Tmax distribution in the definition of HW is intended to detect
173 patterns in the data that deviate from expected patterns. However, the expected patterns

¹ Please, refer to the Appendix for further comparisons.

² Please, refer to the Appendix for further definitions.

174 change over time. In particular, climate change has led to increased average air
175 temperature, a shift of the natural limits, and more frequent high air temperature
176 anomalies (Trenberth *et al*, 2012). Due to climate change, use of a specific reference
177 period may lead to misleading results. Therefore, it is necessary to frequently update the
178 reference period to provide a more meaningful indicator of current weather conditions,
179 as the WMO recommends.

180 The reference period clearly affects the identification of a HW, and yet the
181 official definition of a HW uses a fixed reference period. Therefore we evaluated the
182 extent to which the reference period affects the identification of anomalous air
183 temperatures. In particular, we compared the results from use of the 1971-2000 fixed
184 reference period with use of a 30-year moving reference period (in which the reference
185 period is continuously updated).

186 Second, we also propose to change the period during which the threshold air
187 temperature is computed. Following AEMET's definition of HW, the threshold air
188 temperature is the 95th percentile of the series of daily Tmax values for the months of
189 July and August. This definition means that a HW outside of the summer months (warm
190 spells) is highly improbable. Nonetheless, non-summer air temperatures may be much
191 warmer than expected, but still not exceed this limit. We are interested in detecting
192 anomalously warm data in a specific context ("contextual anomalies"), so propose
193 defining a specific threshold for each day that is computed in accordance with its
194 context. Thus, we do not use a common threshold air temperature for all Julian days,
195 and neither does IPCC definition of HW, but IPCC maintain the same daily threshold
196 for many years (30).

197 Instead, for each Julian day, we propose calculation of a running average of the
198 Tmax of the specific day with the two adjacent days (this reduces day-to-day

199 fluctuations) for all 30 previous calendar dates. The upper daily threshold air
200 temperature for each day is the 95th percentile of the corresponding Tmax series.
201 Climatologists commonly use this criterion to determine the threshold of climate
202 variables (Manton et al. 2001, Labajo et al. 2008).

203 Formally, we define $Tmax_{i,t}$ as the Tmax of the i Julian day of year t and
204 $\widetilde{Tmax}_{i,t}$ as the Tmax series of the Julian day i and the two adjacent days ($Tmax_{i-1,t}$
205 $Tmax_{i+1,t}$) during the previous 30 years.

206 Therefore

$$\widetilde{Tmax}_{i,t} = \{Tmax_{i,j}, Tmax_{i-1,j}, Tmax_{i+1,j} | j = t - 30, t - 29, \dots, t - 1\}$$

207 We also define $P95_{max,i,t}$ as the 95th percentile of $\widetilde{Tmax}_{i,t}$.

208 ***Definition of HW based on moving reference period and daily threshold***

209 ***(MRDT):*** a period of at least 3 consecutive days in which $Tmax_{i,t} > P95_{max,i,t}$.

210 The Tmax threshold in this definition varies with the Julian day (this filters out
211 seasonality, so no correction of values measured directly at an observatory is necessary)
212 and year (this detrends the threshold, and updates it to current conditions), so it
213 incorporates the two key features proposed above.

214

215 3. Data

216 We used daily air temperature data from five observatories from the official network of
217 observatories of the Spanish state in Malaga Province (Spain), which represent a variety
218 of geographical settings (coastal, mountain and inland), for analysis of our alternative
219 definition of HW (Figure 1). The air temperature data at these observatories (Algarrobo,
220 Bobadilla, Cortes de la Frontera, Guadalhorce, Málaga airport) are highly reliable for
221 the period 1971-2016. All data were from AEMET. Mediterranean basin ecosystems are
222 a hotspot of the world's biodiversity and supply numerous services to people, including

223 clean water, flood protection, carbon storage, and recreation. A specific climate zone
224 that has significant inter-annual variability in precipitation and air temperature. In recent
225 decades, there has been severe economic damage and loss of life due to droughts,
226 flooding events, and heat or cold waves, and these may have been exacerbated by
227 increases in population and construction (Easterling *et al.*, 2000). Alpert *et al.* (2002)
228 analyzed observational databases from several areas of the Mediterranean basin using
229 data from the 20th century, and reported an increase in extreme events. The rate of
230 increase in the temperature of the Mediterranean due to the global change in the Planet
231 has accelerated alarmingly in the last 5 to 10 years, at a rate of 0.75 degrees per year,
232 despite the fact that it had been increasing one degree Celsius each 25 years (Guiot and
233 Cramer, 2016).

234 We analyzed the frequency of HWs for 2001-2016, because 1971-2000 data is
235 used as a reference period for computation of Tmax thresholds during the first year
236 (2001), and the reference period is updated for all subsequent years. There were 16790
237 daily values at each of the 5 observatories.

238

239 **4. Results and discussion**

240 We evaluated the sensitivity of the identification of air temperature anomalies with our
241 proposed definition of HW in the data from 5 observatories in Spain. The main features
242 of our new HW definition are that it uses a moving reference period (instead of a fixed
243 reference period) and it uses a specific threshold air temperature for each calendar date
244 (instead of a common fixed threshold air temperature for all dates).

245 Figure 2 compares the number of HWs based on the AEMET definition, our first
246 proposed definition (MRDT), and the IPCC definition.³ We modified the IPCC

³ Please, refer to the Appendix for further comparisons.

247 definition to make it comparable with the MRDT and the AEMET definitions by
248 considering a period of more than 3 consecutive days and by considering the 1971-2000
249 reference period (as in AEMET).

250 There are two main results shown in this figure: first and obvious, there were
251 significantly more HWs using the MRDT definition than the AEMET definition; and
252 second, there were more HWs using the IPCC definition than the MRDT definition. We
253 used the t-test to determine if the difference between the mean number of monthly HWs
254 detected by two measures was significantly different from 0. Therefore, H0 is that two
255 measures had the same result, and H1 is that one of the measures had more HWs than
256 the other. The corresponding t-statistic are respectively, -5.91 $p < 0.0001$; and 2.08 $p =$
257 0.0191 .

258 Figure 3 shows that AEMET only identifies HWs in July, August, and
259 September, whereas the IPCC and MRDT definitions identify HWs in all months of the
260 year also called warm spells, with the greatest frequencies in May and October. Thus, it
261 is more meaningful to define a HW by comparison of daily Tmax with the expected air
262 temperature for the specific Julian day.⁴

263 We propose computing the threshold as the 95th percentile of the series of daily
264 Tmax for the specific Julian day. This allows identification of a Tmax that is warmer
265 than expected for the specific time of the year, but not warmer than the threshold air
266 temperature calculated in the months of July and August (as in the AEMET definition).

267 Figure 4 shows the daily evolution of the threshold for the year 2016 at the
268 Cortes de la Frontera observatory based on the MRDT definition. Note that our
269 methodology does not impose a common threshold air temperature for the same day of

⁴ We have investigated and conclude that these results are not due to a rearrangement of the anomalies. The differences in number of HWs are consistent with a difference in the number of anomalies. We thank an anonymous referee for proposing this verification.

270 different years, in contrast to the IPCC definition that changes the threshold from day to
271 day but it remains fixed for a specific day until the reference period is updated.

272 Figure 4 shows that the thresholds for the IPCC and our proposed method
273 change during the year, and an anomaly is only identified when Tmax is higher than this
274 threshold. Thus, the IPCC and our proposed method identify anomalous high Tmax
275 values that are not identified by AEMET (horizontal line), many of which are in non-
276 summer months.

277 As noted above (Figure 2), the number of HWs based on the IPCC definition is
278 greater than the number from our MRDT proposal, possibly due to differences in their
279 definitions of threshold. IPCC defines an anomaly as any Tmax that is more than 5°C
280 above the mean daily Tmax. In contrast, we define an anomaly as any Tmax that
281 exceeds the $P95_{max,i,t}$ of the $T_{max,\gamma,t}$. We question whether use of a constant difference
282 with respect to the mean (as in the IPCC definition) is the best method to define the
283 threshold. Depending on the distribution of the daily Tmax, 5°C can represent a high or
284 low percentage of the observations.

285 We are trying to identify outliers in our Tmax data (air temperature anomalies),
286 yet outliers skew the mean. Thus, we did not use the mean to identify outliers, because
287 the mean does not represent typical behavior in the presence of outliers. On the
288 contrary, use of the 95th percentile is robust to the presence of extreme outliers.

289 Finally, the MRDT thresholds and the IPCC thresholds change from day to day,
290 adapting to context, but the AEMET threshold is the same for all days. Furthermore, the
291 MRDT and IPCC methods for computing daily threshold are not as stringent as the
292 AEMET method for non-summer months, because the AEMET confines its
293 computation to the months of July and August. In addition, our threshold adapts to the
294 specific context of the day of the year, and also to the overall trend of the series. We

295 propose updating the reference period each year, although the IPCC only updates the
296 reference period every some years.

297 Figure 5 shows the change of the threshold for one specific day (19 May) at the
298 Malaga observatory, calculated using the 3 different definitions of HW, from 2001-
299 2016. It shows that although IPCC uses a different threshold for each day (as in the
300 MRDT definition) and therefore adapts to the context of the Julian day, it does not
301 regularly update the reference period. In contrast, our daily threshold adapts to the
302 history of the 30 previous years. Therefore, we eliminate the arbitrariness of when to
303 update the reference period and avoid abrupt changes in the air temperature thresholds
304 due to the update of the period every 30 or 10 years. Changes in the threshold could
305 make classify a Tmax as anomalous if a reference period is considered, but not if the
306 reference period is updated. These changes are more abrupt the longer the time between
307 updates. Nonetheless, our proposal allows for a continuous change in the air
308 temperature thresholds, avoiding abrupt changes in the thresholds as compared with the
309 updating every 30 years

310 We observed in Figure 5 that the MRDT threshold increased over time. This is
311 because updating of the threshold considers the increment in the daily Tmax for the 19
312 May during the 30 previous years. We believe that use of a moving reference period
313 provides a more meaningful characterization of HWs, because it detrends the time
314 series, and this is important when interpreting weather phenomena. Figure 6 shows the
315 difference of the daily MRDT thresholds from 2001 to 2016 at the Malaga observatory
316 on all 365 Julian days, where positive values mean there was an increase in the MRDT
317 threshold from 2001-2016. Moreover, this figure shows that most of the values were
318 positive (76.4%, 279 out of 365) and the mean difference was also positive (0.504°C).

319 In other words, there was an increase of the MRDT thresholds from 2001-2016 due
320 regular updating.

321

322 **5. Expanded definition of heat wave: second proposal**

323 As have been shown the HW activity has received considerable attention, especially
324 following the European heat waves in 2003 (Beniston and Diaz 2004; Schar *et al.* 2004;
325 Stott *et al.* 2004; Meehl and Tebaldi 2004; Gershunov and Douville 2008). Most studies
326 have focused on local extreme temperature magnitudes and durations associated with
327 heat waves (Beniston 2004; Beniston and Diaz 2004; Schar *et al.* 2004). However, heat
328 waves are inherently regional phenomena with regional impacts. Therefore, the spatial
329 scale of heat waves amplifies the event's stressful effects by spreading them over
330 broader sectors of ecosystems, society, and infrastructure (Gershunov *et al.*, 2009)

331 A more precise and useful description of heat wave activity should include an
332 explicit and separate quantification of daily and nightly temperature extremes. During a
333 persistent daytime heat wave, cool nights provide respite from the stressful effects of
334 heat on the health and general well-being of plants and animals, as well as for the
335 energy sector, and prepare society and nature to face another day of scorching heat.
336 Health impacts of nighttime heat are less well known, but there are indications that high
337 minimum temperatures during heat waves enhance morbidity and mortality (Hémon and
338 Jouglé 2003; Grize *et al.* 2005; Gosling *et al.* 2008; Gershunov *et al.*, 2009).

339 To describe the spatial extent of heat waves and differential symptoms during
340 day and night, we start with maximum and minimum daily air temperatures (T_{max} and
341 T_{min}, respectively) recorded at the 5 representative observatories from the province of
342 Málaga. The minimum and maximum temperatures were hence collected as pertinent

343 indicators of the potential impact of the HW, according with the described
344 methodology.

345 HWs were always characterized by a steep increase of maximum and minimum
346 temperatures and duration of several days. The final choice of a combined indicator
347 “Tmin and Tmax” is consistent with the literature. Indeed, it has already been observed
348 that the maximum temperature alone was not sufficient to estimate the health risk. An
349 elevated by-night temperature not allowing the body to rest is also a key risk factor
350 (Besancenot 2002; Pascal *et al.*, 2006).

351 Taking in account these evidences, we also propose a second method to define a
352 HW, which incorporates analysis of minimum daily air temperatures (Tmin). We
353 propose two alternative definitions based on a moving reference period and two daily
354 thresholds (for Tmax and Tmin), so we designate it as MR2DT. According to the
355 MR2DT(OR), a HW is a period of at least 3 consecutive days in which the Tmax is
356 above the 95th percentile of the series of daily Tmax for the specific Julian day, or in
357 which the Tmin is above the 95th percentile of the series of daily Tmin for the specific
358 Julian day. In the same line, MR2DT(AND) imposes that both thresholds should be
359 exceeded simultaneously.⁵ MR2DT(AND) defines a HW as the period of at least 3
360 consecutive days in which the Tmax is above the 95th percentile of the series of daily
361 Tmax for the specific Julian day, and in which the Tmin is above the 95th percentile of
362 the series of daily Tmin for the specific Julian day.

363 These definitions thus consider maximum and minimum air temperatures, and
364 the Tmax and Tmin thresholds vary with the Julian day and year. The MR2DT(OR) and
365 MR2DT(AND) therefore incorporate the two novelties we first proposed.

367 ($Tmin_{i-1,t}$ $Tmin_{i+1,t}$) during the previous 30 years:

$$\widetilde{Tmin}_t = \{Tmin_{i,j}, Tmin_{i-1,j}, Tmin_{i+1,j} | j = t - 30, t - 29, \dots, t - 1\}$$

368 And $P95_{min,i,t}$ is the 95th percentile of \widetilde{Tmin}_t

369 *Definition of HW based on moving reference period and two alternative daily*
370 *thresholds (MR2DT(OR))*: a period of at least three consecutive days, in which
371 $T_{max_{i,t}} > P95_{i,t}$ or $T_{min_{i,t}} > P95_{i,t}$.

372 *Definition of HW based on moving reference period and two simultaneous*
373 *daily thresholds (MR2DT(AND))*: a period of at least three consecutive days, in which
374 $T_{max_{i,t}} > P95_{i,t}$ and $T_{min_{i,t}} > P95_{i,t}$.

375 Figure 7 shows the number of HWs per year according to the MRDT,
376 MR2DT(OR) and the MR2DT(AND). Obviously, the MR2DT(OR) definition identified
377 more HWs than the MRDT definition because it considers Tmax or Tmin alternatively,
378 while the opposite takes place for the MR2DT(AND) definition, that identified less
379 HWs than the MRDT definition, because it considers Tmax and Tmin simultaneously.
380 Additional interesting results from comparison of the MRDT and MR2DT(OR)
381 definitions are that the HWs in 2007 were mostly due to high Tmax values, the HWs in
382 2004 were mostly due to high Tmin values, and 2015 had many HWs with high Tmax
383 and Tmin values. MR2DT(AND) shows that in 2010 and from 2014 onwards there were
384 more frequency of HWs where Tmax and Tmin threshold temperatures were exceeded.

385 Figure 8 shows the same information with aggregation by month. The MRDT
386 definition identified fewer HWs in the summer months than the MR2DT(OR),
387 especially during June (due to the many high Tmin values in June). The MR2DT(OR)
388 also identified more HWs than the MRDT in July, August, and October, months that
389 also had many anomalous high Tmin values. Nonetheless, MR2DT(AND) identified
390 more number of HWs that exceeds Tmax and Tmin thresholds simultaneously, in
391 March, July, November and December.

392

393 **6. Conclusions**

394 This study shows that modifying some of the criteria used to define a HW
395 provides a more meaningful analysis of monthly and annual changes in HWs. Our
396 evaluation shows that bias is introduced when the definition of a HW is based on a fixed

397 reference period and when the threshold air temperature is the same for all months.
398 Thus, we first suggest use of a moving reference period and a daily Tmax threshold to
399 define a HW (MRDT definition). This allows a more meaningful identification of HWs,
400 because it considers the daily context and long-term changes in climate. Therefore we
401 eliminate the arbitrariness of when to update the reference period, because we propose a
402 continuous update and avoid abrupt changes in the air temperature thresholds due to the
403 update of the period every 30 or 10 years. We further propose defining a HW by
404 analysis of daily Tmax and Tmin, because Tmin provides a more accurate assessment of
405 thermal discomfort.

406 According to the first definition of a HW (MRDT), there were HWs in all years
407 from 2001-2016, and the greatest number of HWs was in 2015 (20 HWs). Moreover,
408 our analysis of HWs throughout the year shows that HWs do not only occur during
409 warm periods (as with the AEMET definition). In fact, the months with the most HWs
410 (warm spells) were May and October.

411 According to our second definition of a HW (MR2DT(OR)), the greatest number
412 of HWs was in 2015 (42 HWs). In addition, based on the MR2DT(OR) definition of
413 HW, there were more HWs during the summer months, with HWs mainly due to
414 anomalous high Tmin. Being more restrictive, a third definition (MR2DT(AND))
415 imposing two simultaneous thresholds (one for Tmax and other for Tmin) shows that
416 more HWs are identified from 2014 onwards.

417

418 **7. Acknowledgements**

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421

422 **8. Appendix. Robustness analysis**

423 In this section we first compare the results of the analysis using the definition MRDT
424 proposed in this paper with the one that use an alternative threshold: the 90th percentile

425 centered on a 5-day window (P90-5) instead of the 95th centered on a 3-day window
426 (P95-3) in order to check the robustness of the conclusions obtained in section 4.

427 The comparison of the daily thresholds P90-5 and P95-3 for one observatory is
428 shown in Figure A1. We observe that evidently when imposing a threshold based on
429 the 90th percentile the threshold is lower. This obviously has an impact over the
430 number of HWs reported by year and month. The comparison of the annual number of
431 HWs reported by MRDT(P95-3) and MRDT(P90-5) in Figure A2 shows an 123%
432 overall increase in the number of HWs reported in the period under MRDT(P90-5)
433 compared to MRDT(95-3).

434 The conclusions obtained from Figure 3 in the manuscript and in Figure A3
435 shows similar conclusions. That is, as we report in the manuscript the IPCC and
436 MRDT(90-5) definitions identifies HWs in all months of the year, with the greatest
437 frequencies in May and October. Conclusions still applies for the comparison of the
438 two definitions proposed, MRDT(P90-5) and MR2DT(P95-3).

439 We now evaluate the sensitivity of the identification of air temperature anomalies
440 with our proposed definition of HW, MRDT, with the definition used in the Warm Spell
441 Duration index (WSDI). For this purpose, we adapt MRDT and WSDI definition to
442 make them comparable. We impose a common threshold based on the WSDI definition,
443 the 90th percentile of the series of the Tmax of Julian day i and the four adjacent days (5
444 day window), named $P90 - 5_{max,i,t}$, for each day i . We define a HW as a period of at
445 least three consecutive days in which $Tmax_{i,t} > P90 - 5_{max,i,t}$. We adapt the
446 definition of MR2DT(OR) and MR2DT(AND) accordingly.

447 We first compare the number of HWs based on the MRDT(P90-5), MR2DT(OR),
448 MR2DT(AND) and WSDI definition (Figure A4) All definitions use the P90-5
449 threshold, but the three former use a moving reference period while the latter a use a
450 fixed referenced period anchored in 1971-2000.

451 We observe that WSDI and MRDT (P90-5) report similar number of HWS but with
452 some differences due to the continuous update of the threshold in MRDT(P90-5)

453 definition. Conclusions regarding to MR2DT(OR) (P90-5) and MR2DT(AND) (P90-5)
454 remain. The first definition report significantly greater number of HWs than the second.
455 It is evident the increase in the number of HWs when considering the MR2DT(OR)
456 (P90-5) definition for 2015, so they are mainly due to the increase in this year of Tmin.

457 Figure A5 shows that WSDI and MRDT(P90-5) definitions identify HWs in all
458 months of the year, with the greatest frequencies in May and October.

459 We conclude from the comparison of both definitions that WSDI report greater
460 number of HWs from May to August while the opposite takes place during the rest of
461 the year. This result must derive from the update of the thresholds that have increased
462 from May to August, while they have reduced from September to April; that is, daily
463 Tmax temperature are higher from May to August than in the period 1971-2000 (Figure
464 A6).

465 Figure A6 shows that although WSDI uses a different threshold for each day (as in
466 the MRDT definition) and therefore adapts to the context of the Julian day, it does not
467 regularly update the reference period) the daily threshold does not change in the period
468 2001-2016. In contrast, our daily threshold adapts to the history of the 30 previous
469 years, so it changes every year. Our proposal allows for a continuous change in the air
470 temperature thresholds, avoiding abrupt changes in the thresholds as compared with the
471 updating every 30 years. This change has made the MRDT (P90-5) threshold from May
472 to August to be higher than the WSDI, therefore reporting a smaller number of HWS
473 during these months.

474 Summing up, we can conclude that the P90-5 threshold is an easier to cross limit, and
475 therefore it reduces its ability to identify extreme situations and would entail very
476 frequent heat warnings. That is why we propose the 95th percentile in a 3-day window
477 threshold that updates every year.

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742 Figure captions:

743 **Figure 1.** Observatories in Malaga Province (Spain).

744

745 **Figure 2.** Number of HWs per year, under different definitions.

746 Note: AEMET: AEMET definition of HW; IPCC: IPCC-adapted from the IPCC definition of HW;

747 MRDT: moving reference, daily threshold definition of HW (proposed in this paper).

748 Source: Based on AEMET daily Tmax data.

749

750 **Figure 3.** Aggregate number of HWs in different months, under different definitions.

751 Note: AEMET: AEMET definition of HW; IPCC: IPCC-adapted from the IPCC definition of HW;

752 MRDT: moving reference, daily threshold definition of HW (proposed in this paper).

753 Source: Based on AEMET daily Tmax data.

754

755 **Figure 4.** Daily thresholds for a HW in 2016 at Algarrobo, under different definitions.

756 Note: AEMET: AEMET definition of HW; IPCC: IPCC-adapted from the IPCC definition of HW;

757 MRDT: moving reference, daily threshold definition of HW (proposed in this paper).

758 Source: Based on AEMET daily Tmax data.

759

760 **Figure 5.** Thresholds for a HW at the Malaga observatory on 19 May, under different
761 definitions.

762 Note: AEMET: AEMET definition of HW; IPCC: IPCC-adapted from the IPCC definition of HW;

763 MRDT: moving reference, daily threshold definition of HW (proposed in this paper).

764 Source: Based on AEMET daily Tmax data.

765

766 **Figure 6.** Difference between the MRDT thresholds in 2001 and 2016.

767 Note: A positive value means the MRDT threshold increased from 2001 to 2016; in other words, there
768 was warming trend during this period.

769

770 **Figure 7.** Number of HWs per year, based on the MRDT and MR2DT definitions.

771 Note: MRDT: moving reference, daily threshold definition of HW (proposed in this paper). MR2DT:

772 moving reference, daily threshold definition of HW considering Tmax and Tmin (proposed in this paper).

773 Source: Based on AEMET daily Tmax data.

774

775 **Figure 8.** Aggregate number of HWs in different months, under MRDT, MR2DT(OR)

776 and MR2DT (AND) definitions.

777 .

778 Note: MRDT: moving reference, daily threshold definition of HW (proposed in this paper). MR2DT:

779 moving reference, daily threshold definition of HW considering Tmax and Tmin (proposed in this paper).

780 MR2DT(OR): moving reference, daily threshold definition of HW considering Tmax and Tmin (proposed

781 in this paper), at least one of the threshold (for Tmax or Tmin) is trespassed. MR2DT(AND): moving

782 reference, daily threshold definition of HW considering Tmax and Tmin (proposed in this paper), both

783 thresholds (for Tmax and Tmin) are trespassed.

784 Source: Based on AEMET daily Tmax data.

785

786 **Figure A1.** Daily thresholds under the different alternatives in observatory 21 for

787 2016.

788 Note: P90-5: daily thresholds using the 90th percentile centered on a 5-day window. P95-3:daily

789 thresholds using the 90th percentile centered on a 5-day window.

790

791 **Figure A2.** Evolution of the frequency of HWs by year under MRDT(P95-3) and

792 MRDT(P90-5).

793 Note: MRDT(P90-5) moving reference, daily threshold definition of HW using the 90th percentile centered on a 5-

794 day window. MRDT(P95-3) moving reference, daily threshold definition of HW using the 95th percentile centered

795 on a 3-day window.

796

797 **Figure A3.** Evolution of the frequency of HWs by month (aggregated data for the period 2001-2016)

798 Note: MRDT(P90-5): moving reference, daily threshold definition of HW using the 90th percentile centered on a 5-

799 day window. MRDT(P95-3): moving reference, daily threshold definition of HW using the 95th percentile centered

800 on a 3-day window.

802

803 **Figure A4.** Evolution of the frequency of HWs by year under alternative definitions

804 Note: WSDI fixed reference, daily threshold definition of HW using the 90th percentile centered on a 5-
805 day window. MRDT(P90-5) moving reference, daily threshold definition of HW using the 90th
806 percentile centered on a 5-day window. MR2DT(OR) (P90-5): moving reference, daily threshold (P90-
807 5) definition of HW considering Tmax and Tmin, at least one of the threshold (for Tmax or Tmin) is
808 trespassed. MR2DT(AND) (P90-5): moving reference, daily threshold (P90-5) definition of HW
809 considering Tmax and Tmin, both thresholds (for Tmax and Tmin) are trespassed.

810

811 **Figure A5.** Evolution of the frequency of HWs by month (aggregated data for the
812 period 2001-2016)

813 Note: WSDI fixed reference, daily threshold definition of HW using the 90th percentile centered on a 5-
814 day window. MRDT(P90-5) moving reference, daily threshold definition of HW using the 90th
815 percentile centered on a 5-day window. MR2DT(OR) (P90-5): moving reference, daily threshold (P90-
816 5) definition of HW considering Tmax and Tmin, at least one of the threshold (for Tmax or Tmin) is
817 trespassed. MR2DT(AND) (P90-5): moving reference, daily threshold (P90-5) definition of HW
818 considering Tmax and Tmin, both thresholds (for Tmax and Tmin) are trespassed.

819

820 **Figure A6.** Daily thresholds for WSDI and MRDT(P90-5) during the period 2001-
821 2016

822 Note: WSDI fixed reference, daily threshold using the 90th percentile centered on a 5-day window.
823 MRDT(P90-5) moving reference, daily threshold using the 90th percentile centered on a 5-day window.

824

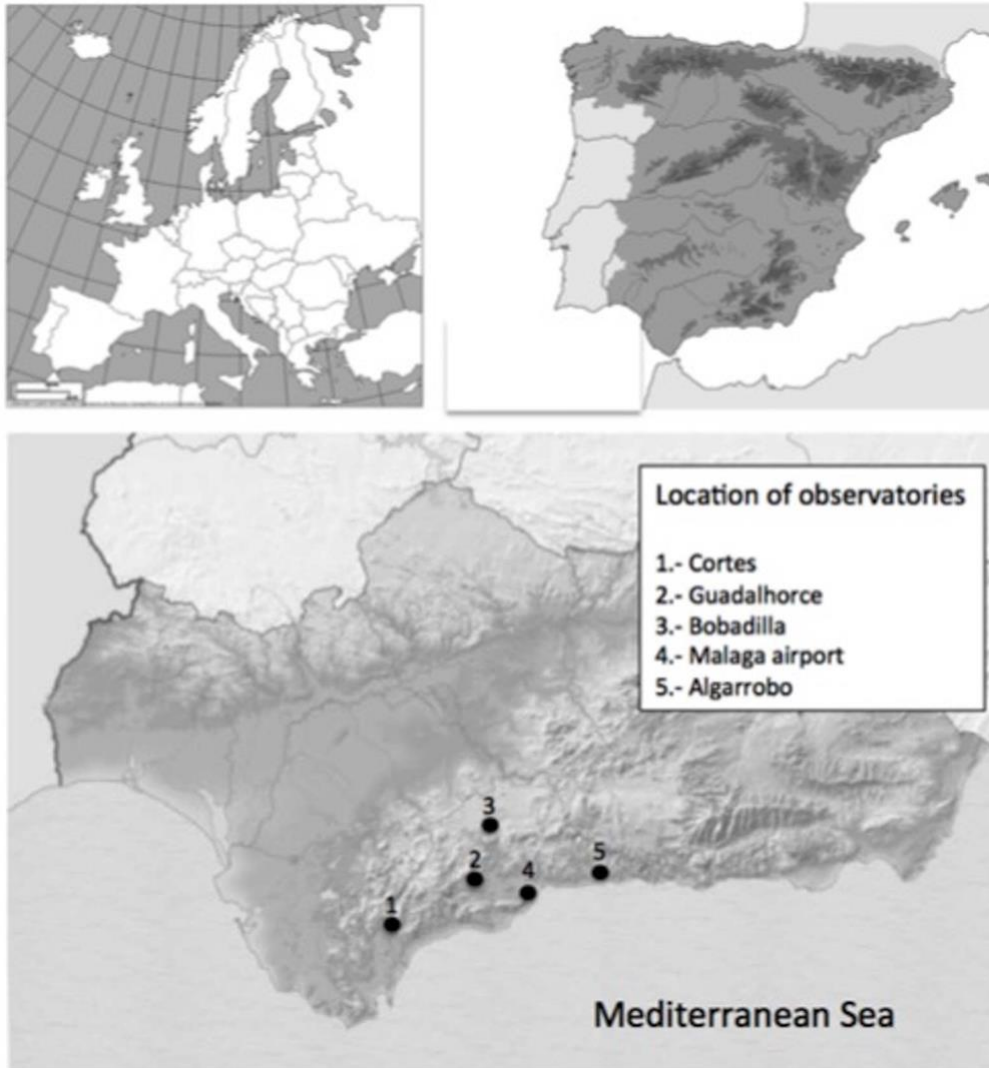


Figure 1.

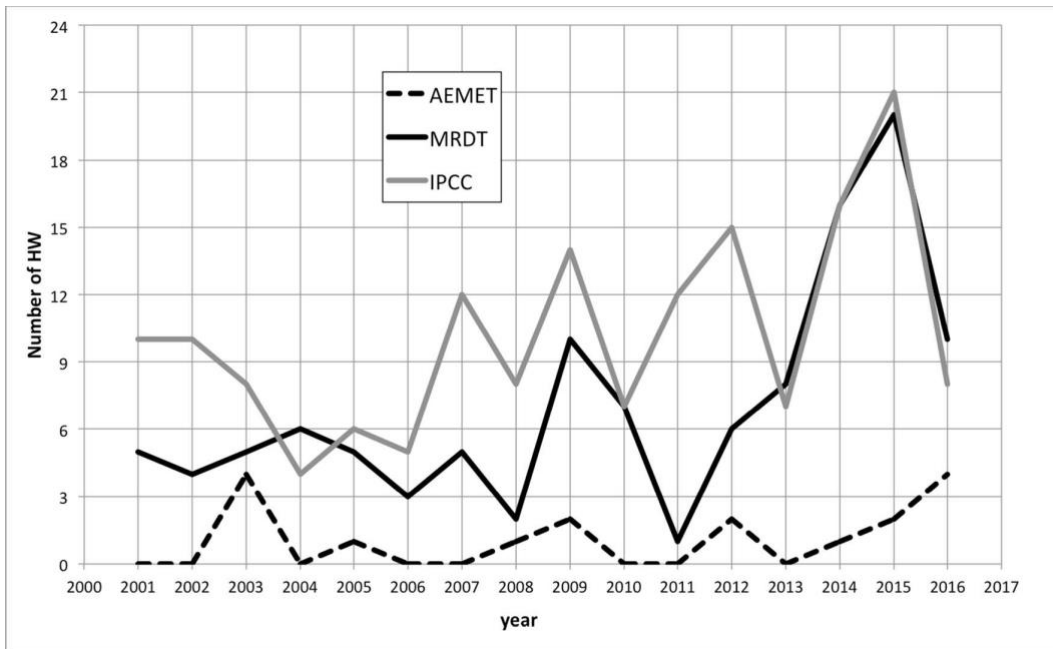


Figure 2. Number of HWs per year, under different definitions.

Figure 3. Aggregate number of HWs in different months, under different definitions.

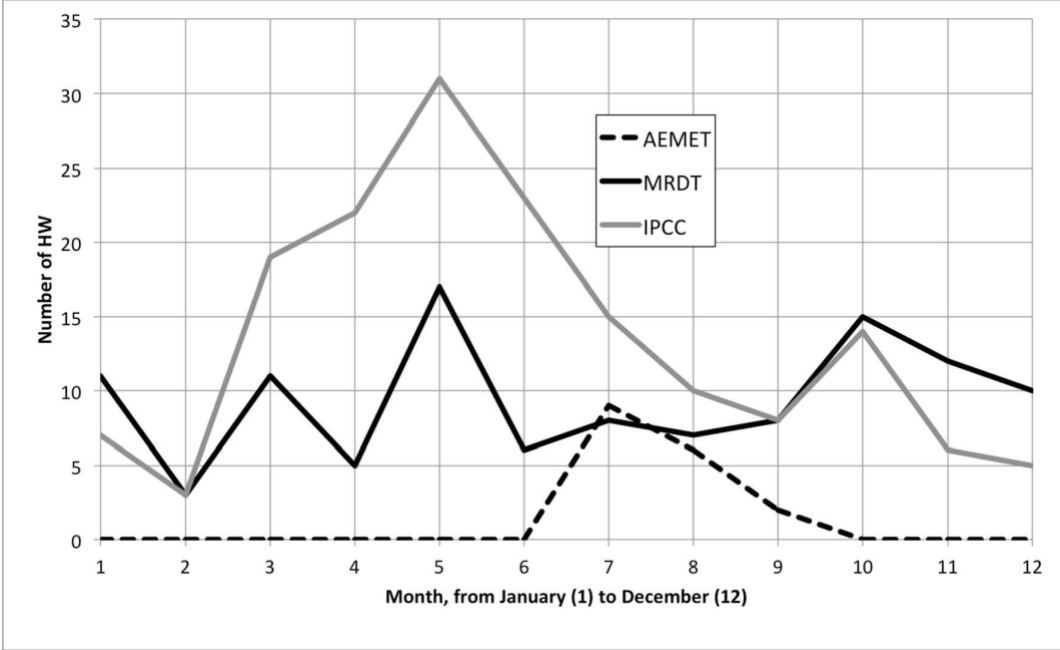


Figure 4. Daily thresholds for a HW in 2016 at Algarrobo, under different definitions

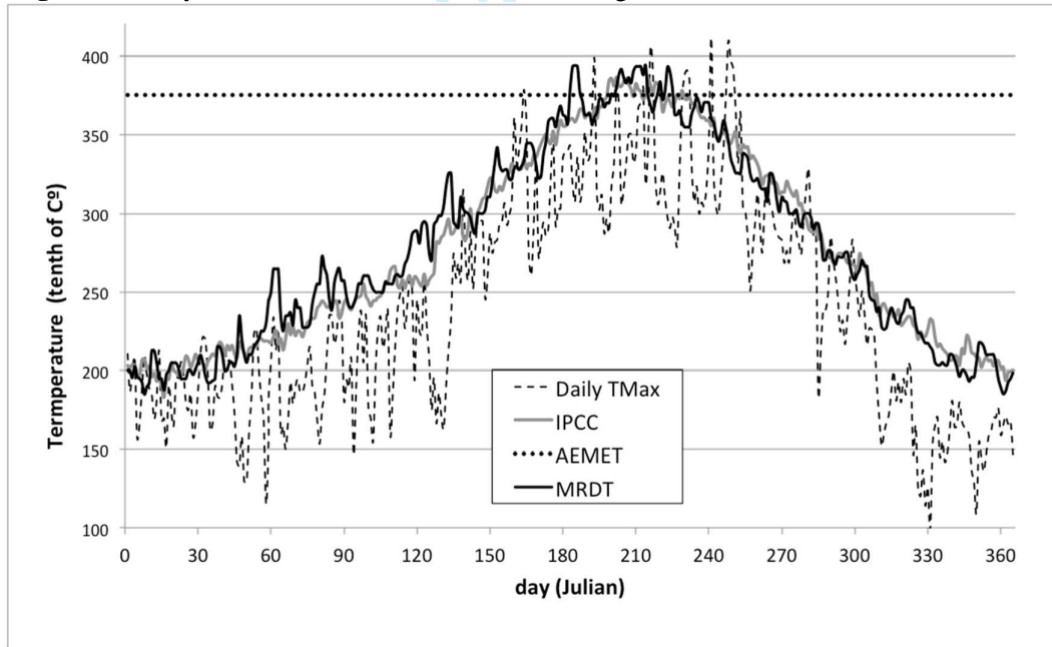


Figure 5. Thresholds for a HW at the Malaga observatory on 19 May, under different definitions.

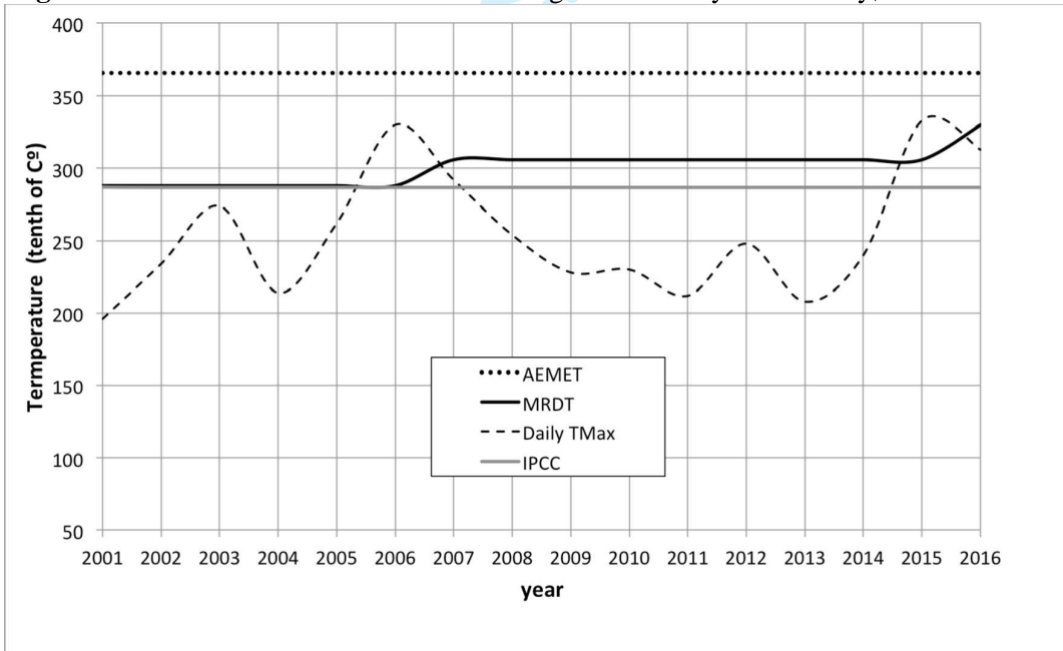
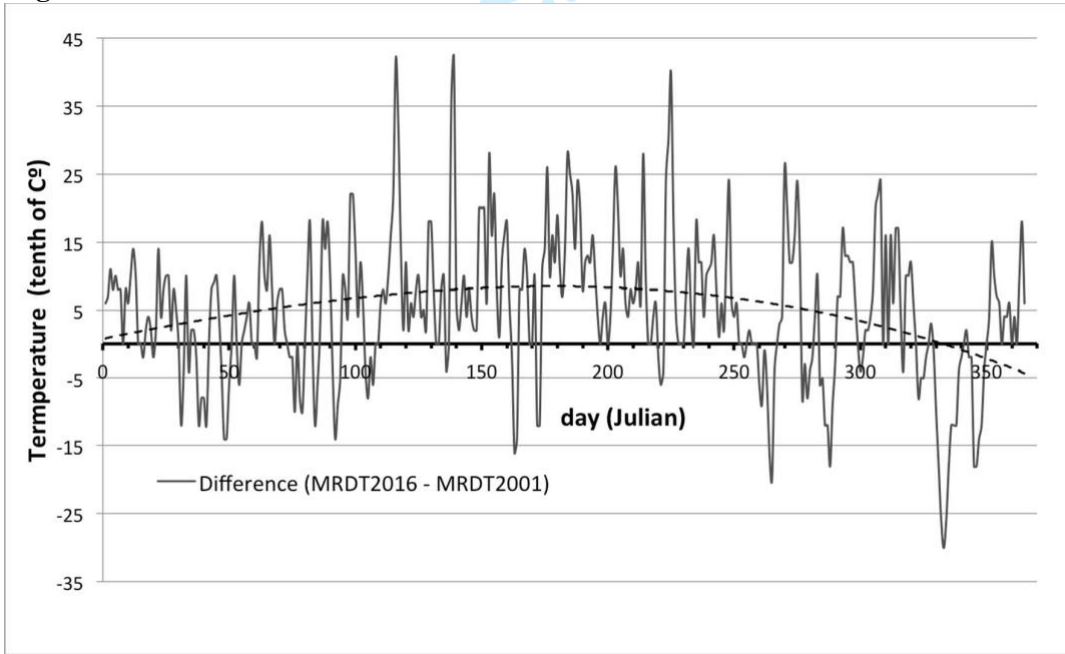


Figure 6. Difference between the MRDT thresholds in 2001 and 2016.



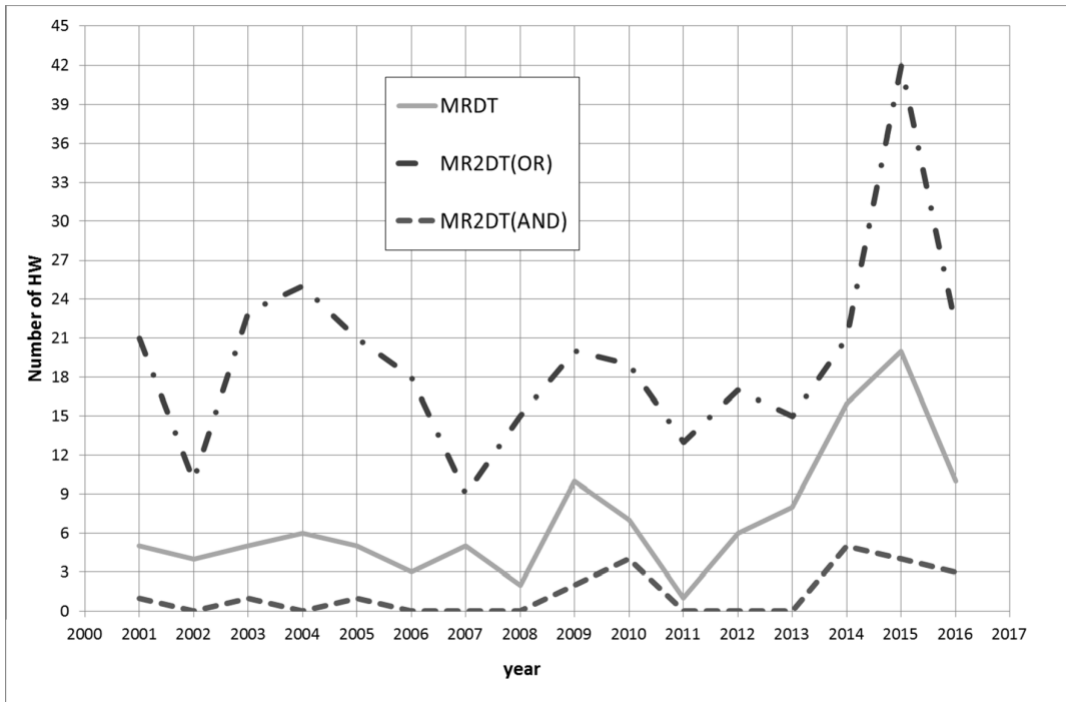


Figure 7. Number of HWs per year, based on the MRDT, MR2DT (OR) and MR2DT (AND) definitions.

Review Only

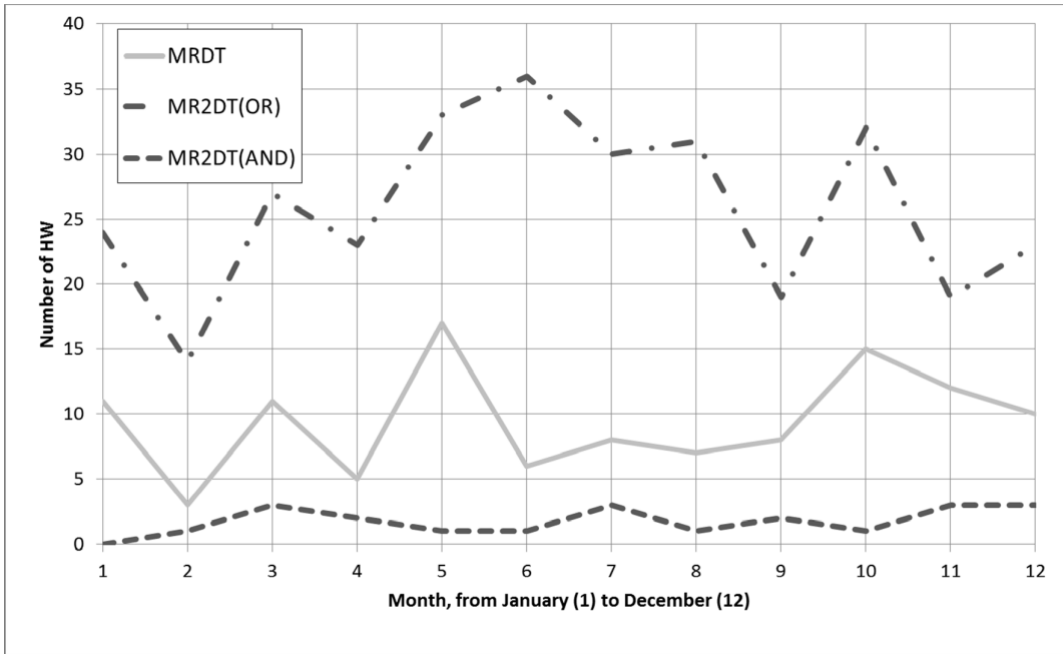


Figure 8. Aggregate number of HWs in different months, under MRDT, MR2DT (OR) and MR2DT (AND) definitions.

Review Only

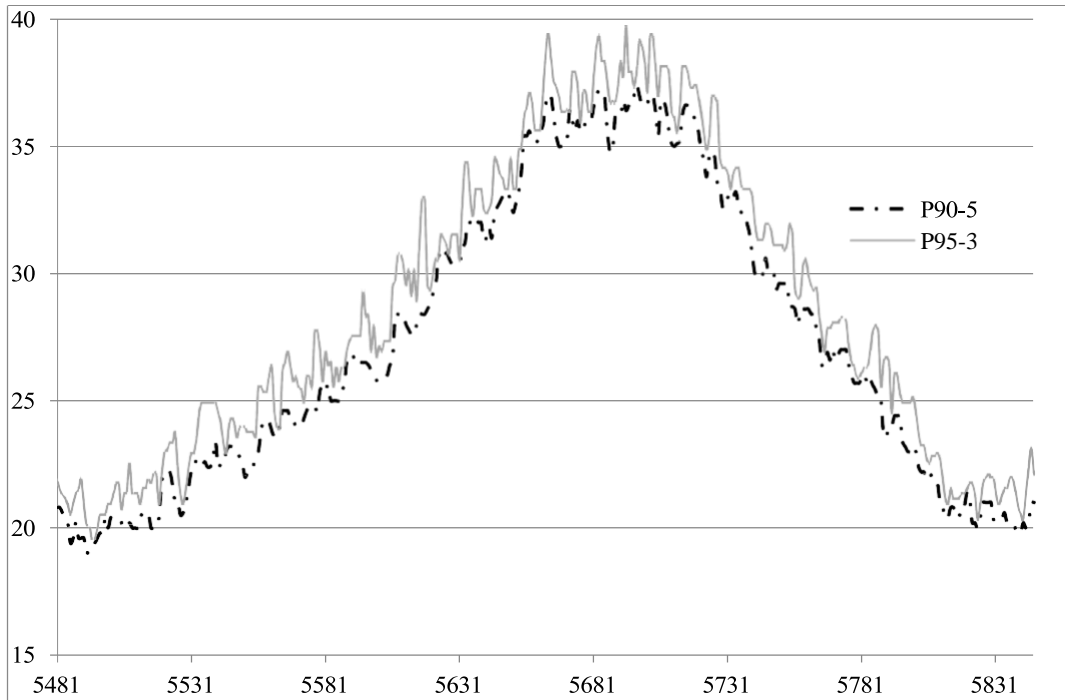


Figure A1. Daily thresholds under the different alternatives in observatory 21 for 2016.

Review Only

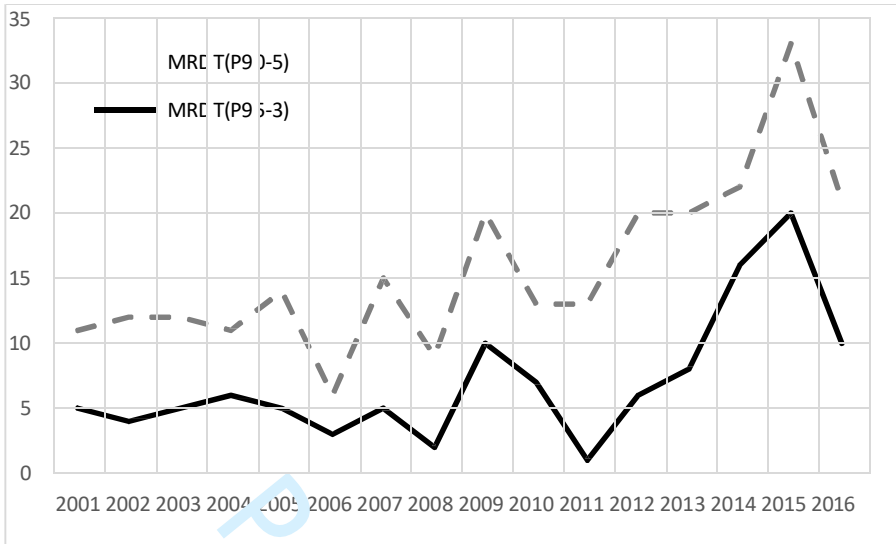


Figure A2. Evolution of the frequency of HWs by year under MRDT(P95-3) and MRDT(P90-5).

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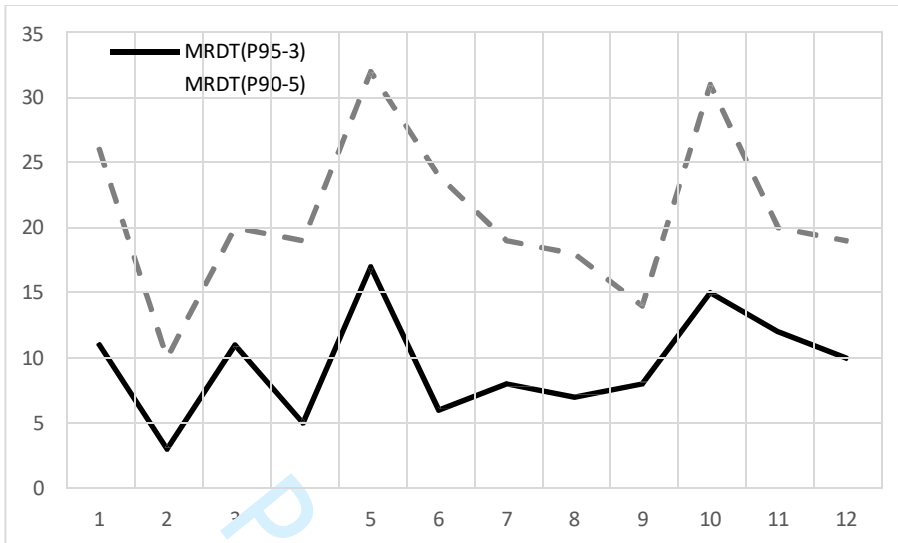


Figure A3. Evolution of the frequency of HWs by month (aggregated data for the period 2001-2016)

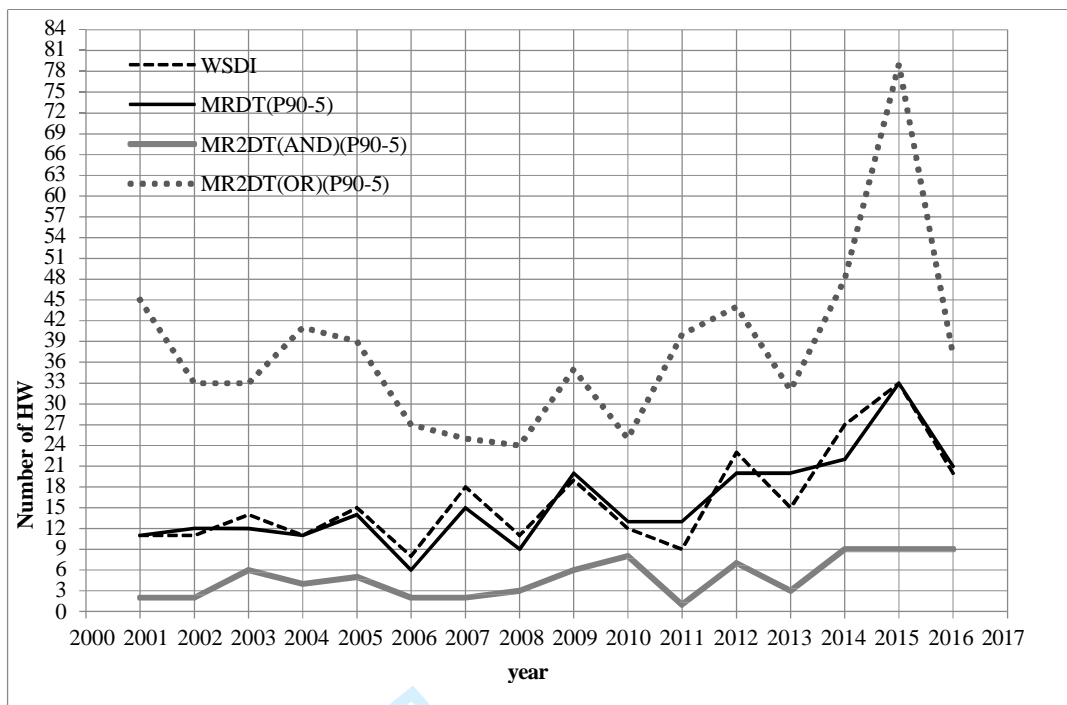


Figure A4. Evolution of the frequency of HWs by year under alternative definitions

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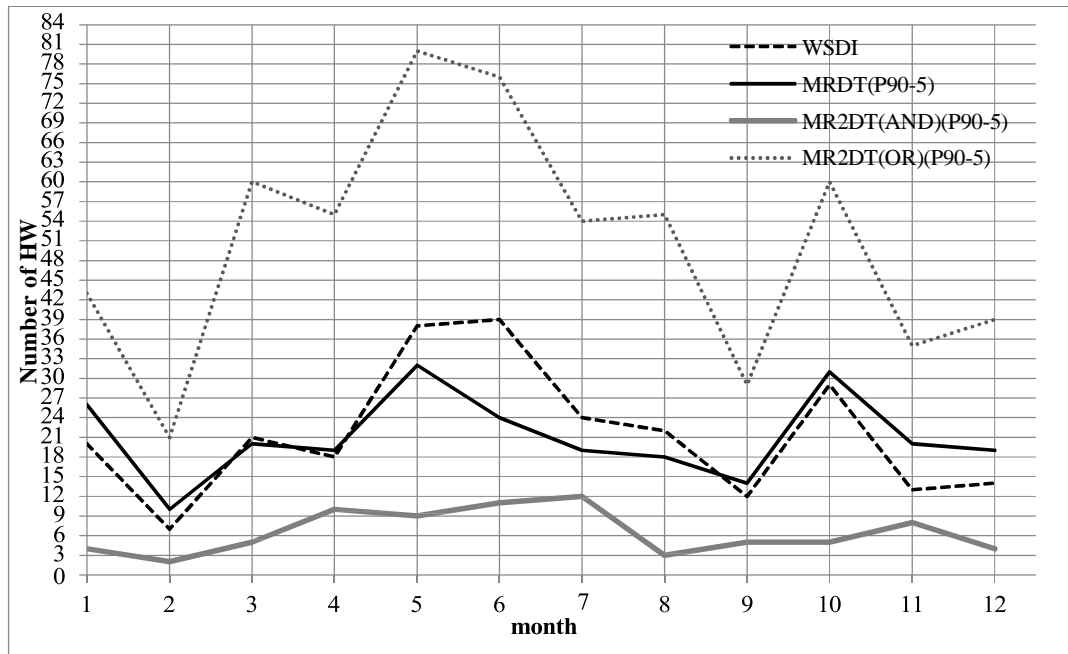


Figure A5. Evolution of the frequency of HWs by month (aggregated data for the period 2001-2016)

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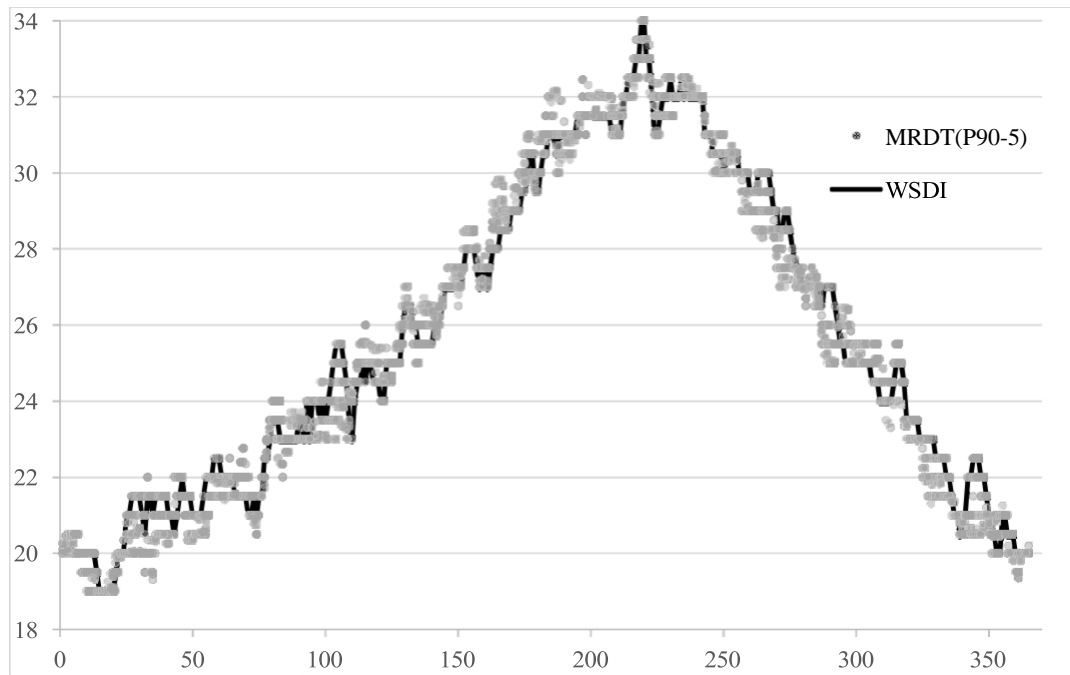


Figure A6. Daily thresholds for WSDI and MRDT(P90-5) during the period 2001-

2016